

一 孤立导体的电容

孤立导体带电荷 Q 与其电势 V 的比值

$$C = \frac{Q}{V}$$

单位: $1 \text{ F} = 1 \text{ C/V}$

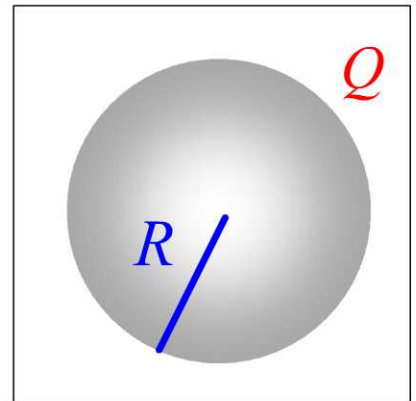
$$1 \text{ F} = 10^6 \mu\text{F} = 10^{12} \text{ pF}$$



例 球形孤立导体的电容

$$V = \frac{Q}{4\pi\epsilon_0 R}$$

$$C = \frac{Q}{V} = 4\pi\epsilon_0 R$$



◆ 地球 $R_E = 6.4 \times 10^6 \text{ m}$, $C_E \approx 7 \times 10^{-4} \text{ F}$



二 电容器

1 电容器分类

按形状：柱型、球型、平行板电容器

按型式：固定、可变、半可变电容器

按介质：空气、塑料、云母、陶瓷等

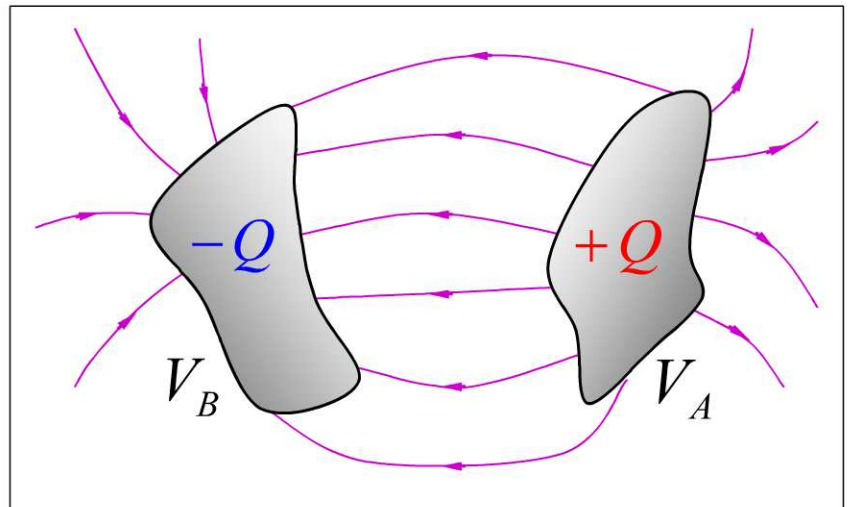
特点：非孤立导体，由两极板组成



2 电容器电容

$$C = \frac{Q}{V_A - V_B} = \frac{Q}{U}$$

$$U = \int_{AB} \vec{E} \cdot d\vec{l}$$



电容的大小仅与导体的**形状**、**相对位置**、**其间的电介质**有关，与所带电荷量**无关**。

3 电容器电容的计算

步骤

$$C = \frac{Q}{V_A - V_B} = \frac{Q}{U}$$

- (1) 设两极板分别带电 $\pm Q$
- (2) 求两极板间的电场强度 \bar{E}
- (3) 求两极板间的电势差 U
- (4) 由 $C=Q/U$ 求 C

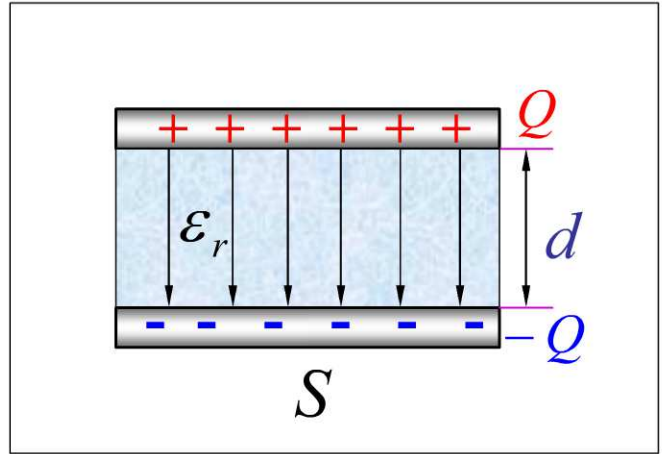


例1 平行平板电容器

解
$$E = \frac{\sigma}{\epsilon_0 \epsilon_r} = \frac{Q}{\epsilon_0 \epsilon_r S}$$

$$U = Ed = \frac{Qd}{\epsilon_0 \epsilon_r S}$$

$$C = \frac{Q}{U} = \frac{\epsilon_0 \epsilon_r S}{d}$$



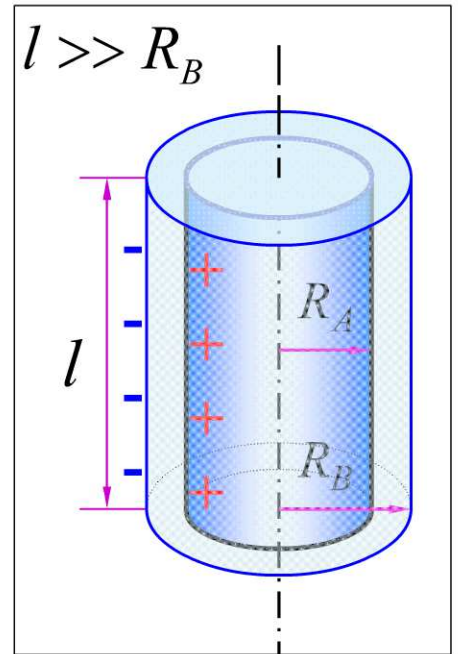
例2 圆柱形电容器

解 设两圆柱面单位长度上分别带电 $\pm\lambda$

$$E = \frac{\lambda}{2\pi\epsilon_0 r} \quad (R_A < r < R_B)$$

$$U = \int_{R_A}^{R_B} \frac{\lambda dr}{2\pi\epsilon_0 r} = \frac{Q}{2\pi\epsilon_0 l} \ln \frac{R_B}{R_A}$$

$$C = \frac{Q}{U} = \frac{2\pi\epsilon_0 l}{\ln \frac{R_B}{R_A}}$$

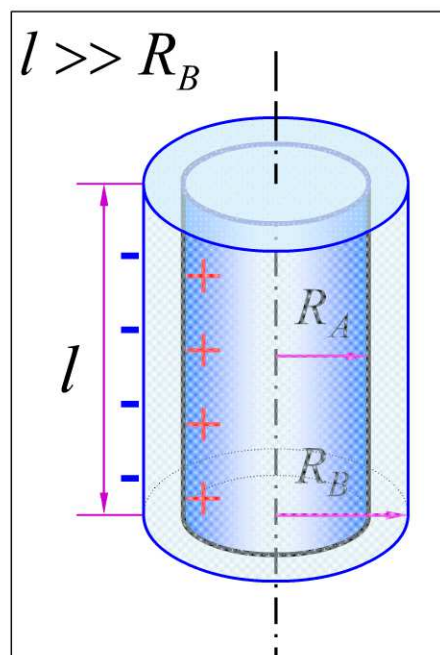


$$C = \frac{Q}{U} = \frac{2\pi\epsilon_0 l}{\ln \frac{R_B}{R_A}}$$

$$d = R_B - R_A \ll R_A$$

$$C \approx \frac{2\pi\epsilon_0 l R_A}{d} = \frac{\epsilon_0 S}{d}$$

平行板电
容器电容



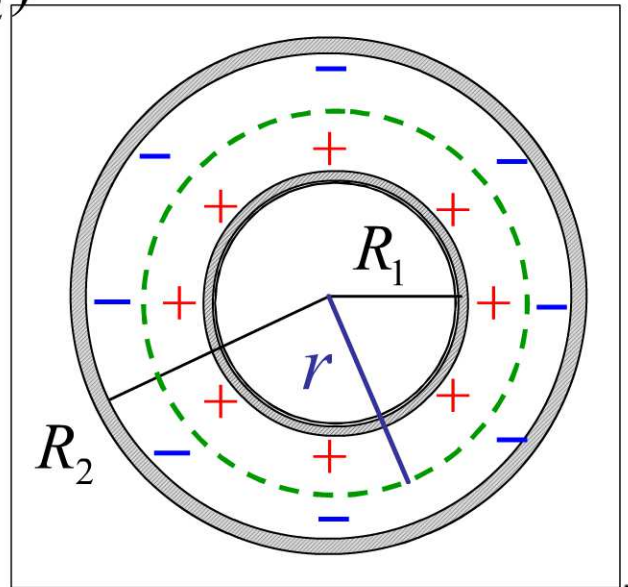
例3 球形电容器的电容**解** 设内外球带分别带电 $\pm Q$

$$E = \frac{Q}{4\pi\epsilon_0 r^2} \quad (R_1 < r < R_2)$$

$$U = \int \vec{E} \cdot d\vec{l}$$

$$= \frac{Q}{4\pi\epsilon_0} \int_{R_1}^{R_2} \frac{dr}{r^2}$$

$$= \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$



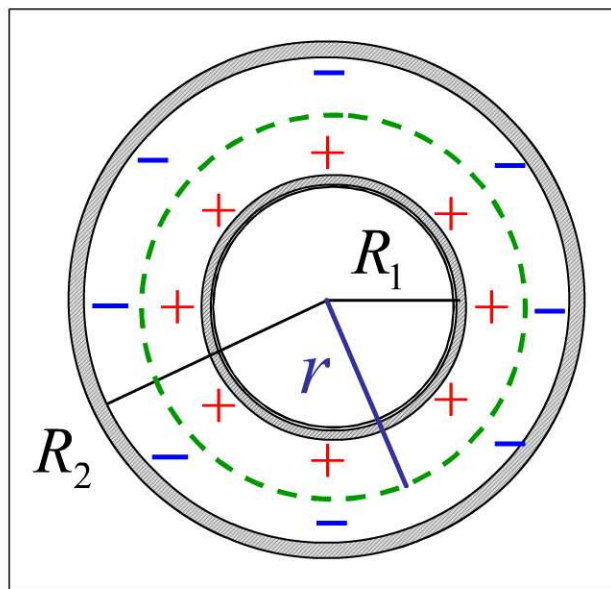
$$U = \frac{Q}{4\pi\epsilon_0} \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$C = \frac{Q}{U} = 4\pi\epsilon_0 \frac{R_1 R_2}{R_2 - R_1}$$

$$R_2 \rightarrow \infty$$

$$C = 4\pi\epsilon_0 R_1$$

孤立导体球电容

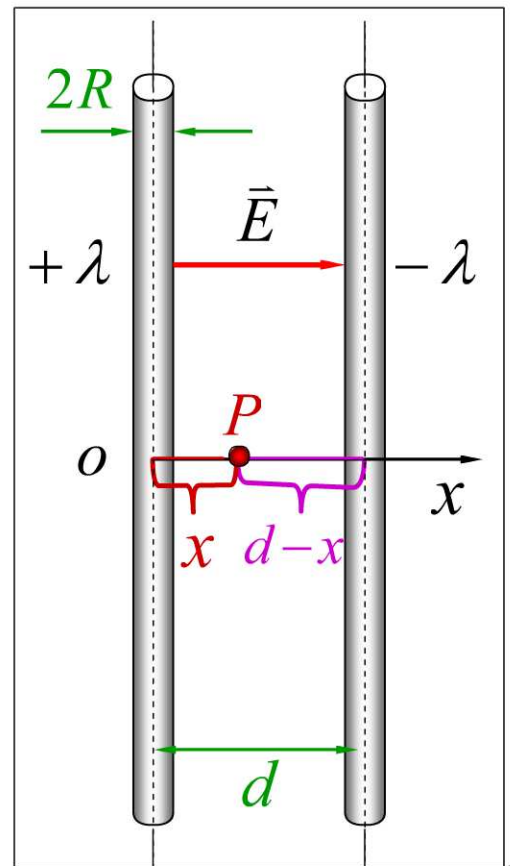


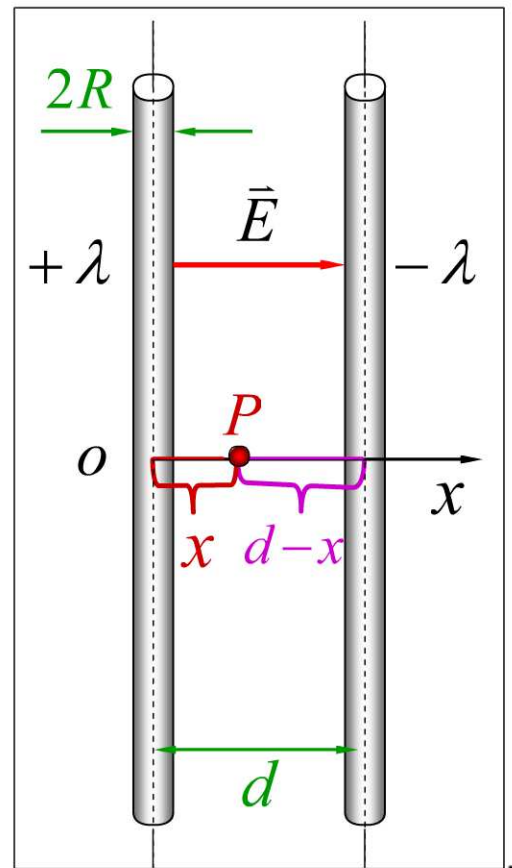
例4 两半径为 R 的平行长直导线，中心间距为 d ，且 $d \gg R$ ，求单位长度的电容。

解 设两金属线的电荷线密度为 $\pm\lambda$

$$E = E_+ + E_-$$

$$= \frac{\lambda}{2\pi\epsilon_0 x} + \frac{\lambda}{2\pi\epsilon_0(d-x)}$$





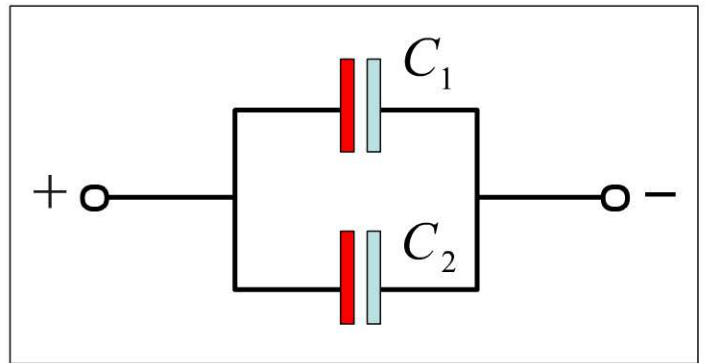
$$\begin{aligned}
 U &= \int_R^{d-R} E dx \\
 &= \frac{\lambda}{2\pi\epsilon_0} \int_R^{d-R} \left(\frac{1}{x} + \frac{1}{d-x} \right) dx \\
 &= \frac{\lambda}{\pi\epsilon_0} \ln \frac{d-R}{R} \approx \frac{\lambda}{\pi\epsilon_0} \ln \frac{d}{R} \\
 C &= \frac{\lambda}{U} = \frac{\pi\epsilon_0}{\ln \frac{d}{R}}
 \end{aligned}$$



三 电容器的并联和串联

1 电容器的并联

$$C = C_1 + C_2$$



2 电容器的串联

$$\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$$

