

波导管 rectangular waveguide

张子珍

山西大同大学物理与电子科学学院

2013.11.17

teaching objectives

- 1 电磁波的传输;

- ① 电磁波的传输;
- ② 波导中电磁波的波动方程及其边界条件;

- ① 电磁波的传输;
- ② 波导中电磁波的波动方程及其边界条件;
- ③ 波导中电磁波的解;

- ① 电磁波的传输;
- ② 波导中电磁波的波动方程及其边界条件;
- ③ 波导中电磁波的解;
- ④ 截止频率;

- ① 电磁波的传输;
- ② 波导中电磁波的波动方程及其边界条件;
- ③ 波导中电磁波的解;
- ④ 截止频率;
- ⑤ TE_{10} 波的电磁场和管壁电流。

- ① 电磁波的传输;
- ② 波导中电磁波的波动方程及其边界条件;
- ③ 波导中电磁波的解;
- ④ 截止频率;
- ⑤ TE_{10} 波的电磁场和管壁电流。

1.电磁能量的传输

- 电路:

1.电磁能量的传输

- **电路**:直流电, **低频**交流电, 日常生活用电;

1. 电磁能量的传输

- **电路**: 直流电, **低频**交流电, 日常生活用电;
- **传输线** (平行双导线, 同轴传输线):

1. 电磁能量的传输

- **电路**: 直流电, **低频** 交流电, 日常生活用电;
- **传输线** (平行双导线, 同轴传输线): **几百兆赫兹**, **厘米波段**, 同轴
线内导体附近电场较强, 大功率应用时容易引起击穿, 传输功率受到限制;

1. 电磁能量的传输

- **电路**: 直流电, **低频** 交流电, 日常生活用电;
- **传输线** (平行双导线, 同轴传输线): **几百兆赫兹**, **厘米波段**, 同轴
线内导体附近电场较强, 大功率应用时容易引起击穿, 传输功率受到限制;
- **波导** (矩形, 圆形):

1. 电磁能量的传输

- **电路**: 直流电, **低频**交流电, 日常生活用电;
- **传输线** (平行双导线, 同轴传输线): **几百兆赫兹**, **厘米波段**, 同轴
线内导体附近电场较强, 大功率应用时容易引起击穿, 传输功率受到限制;
- **波导** (矩形, 园形): **厘米波、毫米波段的大功率传输**;

1. 电磁能量的传输

- **电路**: 直流电, **低频**交流电, 日常生活用电;
- **传输线** (平行双导线, 同轴传输线): **几百兆赫兹**, **厘米波段**, 同轴
线内导体附近电场较强, 大功率应用时容易引起击穿, 传输功率受到限制;
- **波导** (矩形, 园形): **厘米波、毫米波段的大功率传输**;
- **光纤**:

1. 电磁能量的传输

- **电路**: 直流电, **低频**交流电, 日常生活用电;
- **传输线** (平行双导线, 同轴传输线): **几百兆赫兹**, **厘米波段**, 同轴
线内导体附近电场较强, 大功率应用时容易引起击穿, 传输功率受到限制;
- **波导** (矩形, 园形): **厘米波、毫米波段的大功率传输**;
- **光纤**: 光纤损耗小, **传输容量大**, 是信号**远距离**传输的最佳选择.

1. 电磁能量的传输

- **电路**: 直流电, **低频**交流电, 日常生活用电;
- **传输线** (平行双导线, 同轴传输线): **几百兆赫兹**, **厘米波段**, 同轴线内导体附近电场较强, 大功率应用时容易引起击穿, 传输功率受到限制;
- **波导** (矩形, 园形): **厘米波、毫米波段的大功率传输**;
- **光纤**: 光纤损耗小, **传输容量大**, 是信号**远距离**传输的最佳选择.

2. The Equation and Boundary Conditions of Electromagnetic Waves

}

2. The Equation and Boundary Conditions of Electromagnetic Waves

$$\left\{ \begin{array}{l} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \end{array} \right.$$

2. The Equation and Boundary Conditions of Electromagnetic Waves

$$\begin{cases} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \end{cases}$$

2. The Equation and Boundary Conditions of Electromagnetic Waves

$$\left\{ \begin{array}{l} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \\ \frac{\partial E_n}{\partial n} = 0 \end{array} \right.$$

2. The Equation and Boundary Conditions of Electromagnetic Waves

$$\left\{ \begin{array}{l} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \\ \frac{\partial E_n}{\partial n} = 0 \end{array} \right. \quad (1)$$

2.The Equation and Boundary Conditions of Electromagnetic Waves

$$\begin{cases} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \\ \frac{\partial E_n}{\partial n} = 0 \end{cases} \quad (1)$$

方程 (1) 的解必需满足条件

2. The Equation and Boundary Conditions of Electromagnetic Waves

$$\begin{cases} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \\ \frac{\partial E_n}{\partial n} = 0 \end{cases} \quad (1)$$

方程 (1) 的解必需满足条件

$$\nabla \cdot \vec{E} = 0 \quad (2)$$

2.The Equation and Boundary Conditions of Electromagnetic Waves

$$\begin{cases} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \\ \frac{\partial E_n}{\partial n} = 0 \end{cases} \quad (1)$$

方程 (1) 的解必需满足条件

$$\nabla \cdot \vec{E} = 0 \quad (2)$$

在波导管中，受四个面的限制，

2. The Equation and Boundary Conditions of Electromagnetic Waves

$$\begin{cases} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \\ \frac{\partial E_n}{\partial n} = 0 \end{cases} \quad (1)$$

方程 (1) 的解必需满足条件

$$\nabla \cdot \vec{E} = 0 \quad (2)$$

在波导管中，受四个面的限制，
对 E_x ， $\frac{\partial E_x}{\partial x}|_{x=0,a} = 0$ ， $E_x|_{y=0,b} = 0$ ，

2. The Equation and Boundary Conditions of Electromagnetic Waves

$$\begin{cases} \nabla^2 \vec{E} + k^2 \vec{E} = 0 \\ E_t = 0 \\ \frac{\partial E_n}{\partial n} = 0 \end{cases} \quad (1)$$

方程 (1) 的解必需满足条件

$$\nabla \cdot \vec{E} = 0 \quad (2)$$

在波导管中，受四个面的限制，
对 E_x ， $\frac{\partial E_x}{\partial x}|_{x=0,a} = 0$ ， $E_x|_{y=0,b} = 0$ ，

3. Electromagnetic waves in waveguide

$$\text{对 } E_y, \quad \left. \frac{\partial E_y}{\partial y} \right|_{y=0,b} = 0, \quad E_y|_{x=0,a} = 0,$$

3. Electromagnetic waves in waveguide

$$\text{对 } E_y, \quad \frac{\partial E_y}{\partial y} \Big|_{y=0,b} = 0, \quad E_y \Big|_{x=0,a} = 0,$$

$$\text{对 } E_z, \quad E_z \Big|_{x=0,a} = 0, \quad E_z \Big|_{y=0,b} = 0,$$

3. Electromagnetic waves in waveguide

对 E_y , $\frac{\partial E_y}{\partial y}|_{y=0,b} = 0$, $E_y|_{x=0,a} = 0$,

对 E_z , $E_z|_{x=0,a} = 0$, $E_z|_{y=0,b} = 0$,

z 为电磁波的传播方向, 故

3. Electromagnetic waves in waveguide

对 E_y , $\frac{\partial E_y}{\partial y}|_{y=0,b} = 0$, $E_y|_{x=0,a} = 0$,

对 E_z , $E_z|_{x=0,a} = 0$, $E_z|_{y=0,b} = 0$,

z 为电磁波的传播方向, 故

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

3. Electromagnetic waves in waveguide

对 E_y , $\frac{\partial E_y}{\partial y}|_{y=0,b} = 0$, $E_y|_{x=0,a} = 0$,

对 E_z , $E_z|_{x=0,a} = 0$, $E_z|_{y=0,b} = 0$,

z 为电磁波的传播方向, 故

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_y = A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \quad (3)$$

3. Electromagnetic waves in waveguide

对 E_y , $\frac{\partial E_y}{\partial y}|_{y=0,b} = 0$, $E_y|_{x=0,a} = 0$,

对 E_z , $E_z|_{x=0,a} = 0$, $E_z|_{y=0,b} = 0$,

z 为电磁波的传播方向, 故

$$\begin{aligned} E_x &= A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ E_y &= A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ E_z &= A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z} \end{aligned} \quad (3)$$

3. Electromagnetic waves in waveguide

对 E_y , $\frac{\partial E_y}{\partial y}|_{y=0,b} = 0$, $E_y|_{x=0,a} = 0$,

对 E_z , $E_z|_{x=0,a} = 0$, $E_z|_{y=0,b} = 0$,

z 为电磁波的传播方向, 故

$$\begin{aligned} E_x &= A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ E_y &= A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ E_z &= A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z} \end{aligned} \quad (3)$$

且 A_1, A_2, A_3 只有两个是独立的, 因为

3. Electromagnetic waves in waveguide

对 E_y , $\frac{\partial E_y}{\partial y}|_{y=0,b} = 0$, $E_y|_{x=0,a} = 0$,

对 E_z , $E_z|_{x=0,a} = 0$, $E_z|_{y=0,b} = 0$,

z 为电磁波的传播方向, 故

$$\begin{aligned} E_x &= A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ E_y &= A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ E_z &= A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z} \end{aligned} \quad (3)$$

且 A_1, A_2, A_3 只有两个是独立的, 因为

$$\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 - ik_z A_3 = 0 \quad (4)$$

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = i\omega\mu\vec{H} \quad (5)$$

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = i\omega\mu\vec{H} \quad (5)$$

$$\vec{H} = -\frac{i}{\omega\mu}\nabla \times \vec{E}$$

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = i\omega\mu\vec{H} \quad (5)$$

$$\vec{H} = -\frac{i}{\omega\mu} \nabla \times \vec{E} \quad \vec{H} \Rightarrow \frac{\vec{k} \times \vec{E}}{\omega\mu}$$

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = i\omega\mu\vec{H} \quad (5)$$

$$\vec{H} = -\frac{i}{\omega\mu} \nabla \times \vec{E} \quad \vec{H} \Rightarrow \frac{\vec{k} \times \vec{E}}{\omega\mu}$$

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = i\omega\mu\vec{H} \quad (6)$$

$$\vec{H} = -\frac{i}{\omega\mu} \nabla \times \vec{E} \quad \vec{H} \neq \frac{\vec{k} \times \vec{E}}{\omega\mu}$$

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = i\omega\mu\vec{H} \quad (6)$$

$$\vec{H} = -\frac{i}{\omega\mu} \nabla \times \vec{E} \quad \vec{H} \neq \frac{\vec{k} \times \vec{E}}{\omega\mu}$$

$$\vec{H} = -\frac{i}{\omega\mu} \begin{vmatrix} \hat{e}_x & \hat{e}_y & \hat{e}_z \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ E_x & E_y & E_z \end{vmatrix} \quad (7)$$

3. Magnetic field in waveguide

对同一组 (m, n) , 只有两种独立的偏振波模

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} = i\omega\mu\vec{H} \quad (6)$$

$$\vec{H} = -\frac{i}{\omega\mu} \nabla \times \vec{E} \quad \vec{H} \neq \frac{\vec{k} \times \vec{E}}{\omega\mu}$$

$$\vec{H} = -\frac{i}{\omega\mu} \begin{vmatrix} \hat{e}_x & \hat{e}_y & \hat{e}_z \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ E_x & E_y & E_z \end{vmatrix} \quad (7)$$

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$,

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$,

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$, $\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 = 0$

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$, $\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 = 0$

$$H_z = -\frac{i}{\omega\mu} (k_x A_2 - k_y A_1) \cos\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$, $\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 = 0$

$$H_z = -\frac{i}{\omega\mu} (k_x A_2 - k_y A_1) \cos\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$\neq 0$

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$, $\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 = 0$

$$H_z = -\frac{i}{\omega\mu} (k_x A_2 - k_y A_1) \cos\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ \neq 0$$

同样, $H_z = 0$ 时

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$, $\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 = 0$

$$H_z = -\frac{i}{\omega\mu} (k_x A_2 - k_y A_1) \cos\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ \neq 0$$

同样, $H_z = 0$ 时, $E_z \neq 0$

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$, $\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 = 0$

$$H_z = -\frac{i}{\omega\mu} (k_x A_2 - k_y A_1) \cos\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \\ \neq 0$$

同样, $H_z = 0$ 时, $E_z \neq 0$ 所以, 在波导管中只能传播横电波或横磁波,

3. Magnetic field in waveguide

$$H_z = -\frac{i}{\omega\mu} \left(\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} \right) \quad (8)$$

若 $E_z = 0$, 即 $A_3 = 0$, $\frac{m\pi}{a}A_1 + \frac{n\pi}{b}A_2 = 0$

$$H_z = -\frac{i}{\omega\mu} (k_x A_2 - k_y A_1) \cos\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z} \neq 0$$

同样, $H_z = 0$ 时, $E_z \neq 0$ 所以, 在波导管中只能传播横电波或横磁波, 不能传播横电磁波。

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时,

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$,

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$, 当 $k^2 < k_x^2 + k_y^2$ 时,

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$, 当 $k^2 < k_x^2 + k_y^2$ 时, $k_z^2 < 0$,

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$, 当 $k^2 < k_x^2 + k_y^2$ 时, $k_z^2 < 0$, 传播因子就变成衰减因子。

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$, 当 $k^2 < k_x^2 + k_y^2$ 时, $k_z^2 < 0$, 传播因子就变成衰减因子。所以最小的频率为

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$, 当 $k^2 < k_x^2 + k_y^2$ 时, $k_z^2 < 0$, 传播因子就变成衰减因子。所以最小的频率为

$$k^2 = k_x^2 + k_y^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 \quad (10)$$

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$, 当 $k^2 < k_x^2 + k_y^2$ 时, $k_z^2 < 0$, 传播因子就变成衰减因子。所以最小的频率为

$$k^2 = k_x^2 + k_y^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 \quad (10)$$

$$\omega_{mn} = \frac{1}{\sqrt{\mu\varepsilon}} \sqrt{\left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2} \quad (11)$$

4. 截止频率 (cutoff frequency)

$$k^2 = k_x^2 + k_y^2 + k_z^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 + k_z^2 \quad (9)$$

当 $k^2 = k_x^2 + k_y^2$ 时, $k_z^2 = 0$, 当 $k^2 < k_x^2 + k_y^2$ 时, $k_z^2 < 0$, 传播因子就变成衰减因子。所以最小的频率为

$$k^2 = k_x^2 + k_y^2 = \left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2 \quad (10)$$

$$\omega_{mn} = \frac{1}{\sqrt{\mu\varepsilon}} \sqrt{\left(\frac{m\pi}{a}\right)^2 + \left(\frac{n\pi}{b}\right)^2} \quad (11)$$

4. bE_{10} wave electromagnetic field

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$
$$E_y = A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_y = A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_z = A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_y = A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_z = A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

当 $m = 1, n = 0$ 时,

$$E_x = 0,$$

4. bE_{10} wave electromagnetic field

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_y = A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_z = A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

当 $m = 1, n = 0$ 时,

$$E_x = 0,$$

$$E_y = A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

4. bE_{10} wave electromagnetic field

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_y = A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_z = A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

当 $m = 1, n = 0$ 时,

$$E_x = 0,$$

$$E_y = A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$E_z = 0.$$

4. bE_{10} wave electromagnetic field

$$E_x = A_1 \cos\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_y = A_2 \sin\left(\frac{m\pi}{a}x\right) \cos\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

$$E_z = A_3 \sin\left(\frac{m\pi}{a}x\right) \sin\left(\frac{n\pi}{b}y\right) e^{ik_z z}$$

当 $m = 1, n = 0$ 时,

$$E_x = 0,$$

$$E_y = A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$E_z = 0.$$

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$
$$H_y = 0,$$

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$H_y = 0,$$

$$H_z = -\frac{i}{\omega\mu} \frac{\partial E_y}{\partial x} = -\frac{i}{\omega\mu} \left(\frac{\pi}{a}\right) A_2 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$H_y = 0,$$

$$\begin{aligned} H_z &= -\frac{i}{\omega\mu} \frac{\partial E_y}{\partial x} = -\frac{i}{\omega\mu} \left(\frac{\pi}{a}\right) A_2 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \\ &= H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \end{aligned}$$

4. TE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$H_y = 0,$$

$$\begin{aligned} H_z &= -\frac{i}{\omega\mu} \frac{\partial E_y}{\partial x} = -\frac{i}{\omega\mu} \left(\frac{\pi}{a}\right) A_2 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \\ &= H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \end{aligned}$$

TE₁₀是横电波，而不是横磁波。

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$H_y = 0,$$

$$\begin{aligned} H_z &= -\frac{i}{\omega\mu} \frac{\partial E_y}{\partial x} = -\frac{i}{\omega\mu} \left(\frac{\pi}{a}\right) A_2 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \\ &= H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \end{aligned}$$

TE₁₀是横电波，而不是横磁波。

$$H_x = \frac{-ik_z a}{\pi} H_0 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$H_y = 0,$$

$$\begin{aligned} H_z &= -\frac{i}{\omega\mu} \frac{\partial E_y}{\partial x} = -\frac{i}{\omega\mu} \left(\frac{\pi}{a}\right) A_2 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \\ &= H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \end{aligned}$$

TE₁₀是横电波，而不是横磁波。

$$H_x = \frac{-ik_z a}{\pi} H_0 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

$$E_y = \frac{i\omega\mu a}{\pi} H_0 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$H_y = 0,$$

$$\begin{aligned} H_z &= \frac{i}{\omega\mu} \frac{\partial E_y}{\partial x} = -\frac{i}{\omega\mu} \left(\frac{\pi}{a}\right) A_2 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \\ &= H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \end{aligned}$$

TE₁₀是横电波，而不是横磁波。

$$H_x = \frac{-ik_z a}{\pi} H_0 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

$$E_y = \frac{i\omega\mu a}{\pi} H_0 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

$$H_z = H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field

$$H_x = \frac{i}{\omega\mu} \frac{\partial E_y}{\partial z} = -\frac{k_z}{\omega\mu} A_2 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z},$$

$$H_y = 0,$$

$$\begin{aligned} H_z &= -\frac{i}{\omega\mu} \frac{\partial E_y}{\partial x} = -\frac{i}{\omega\mu} \left(\frac{\pi}{a}\right) A_2 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \\ &= H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z} \end{aligned}$$

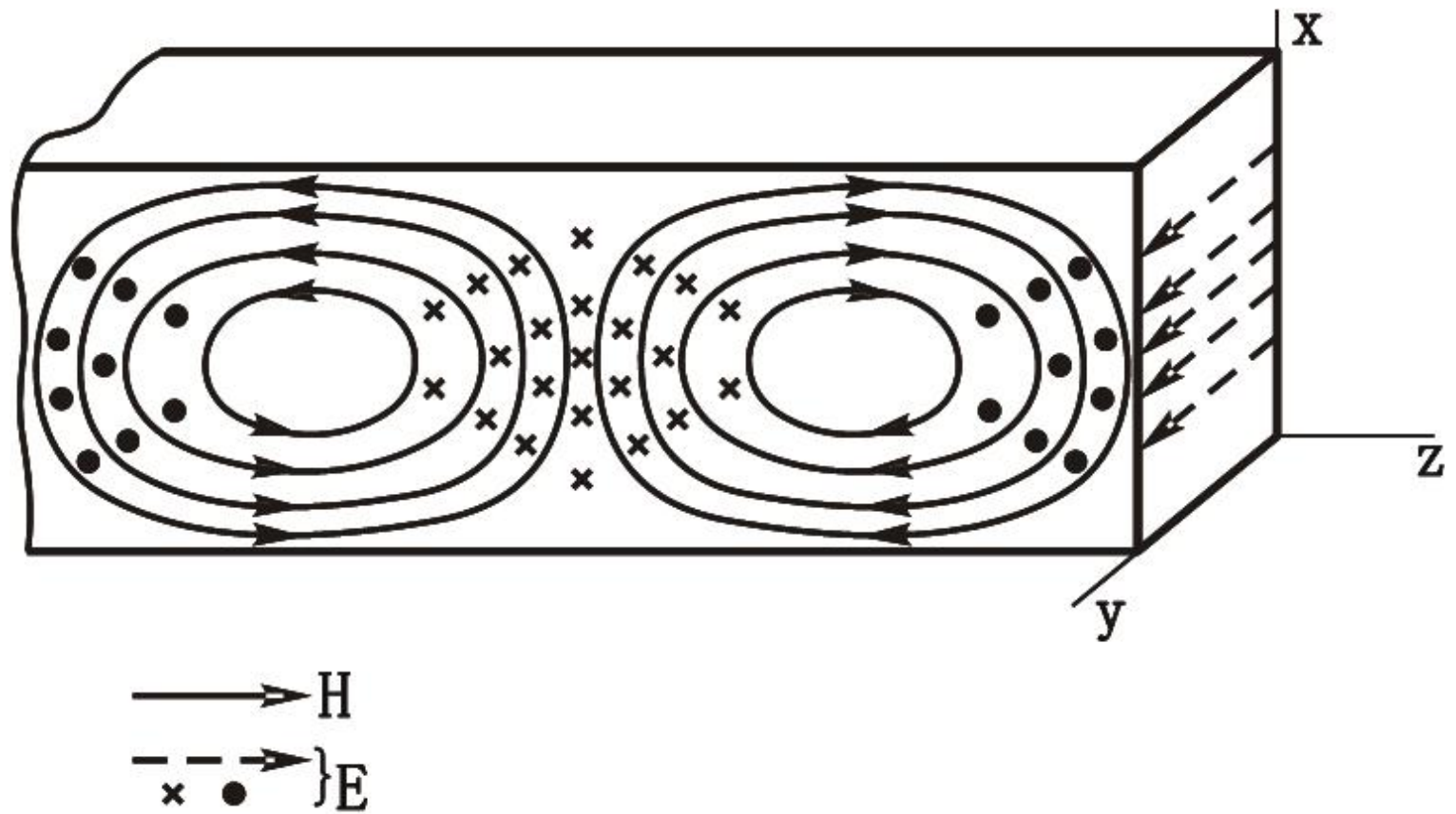
TE₁₀是横电波，而不是横磁波。

$$H_x = \frac{-ik_z a}{\pi} H_0 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

$$E_y = \frac{i\omega\mu a}{\pi} H_0 \sin\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

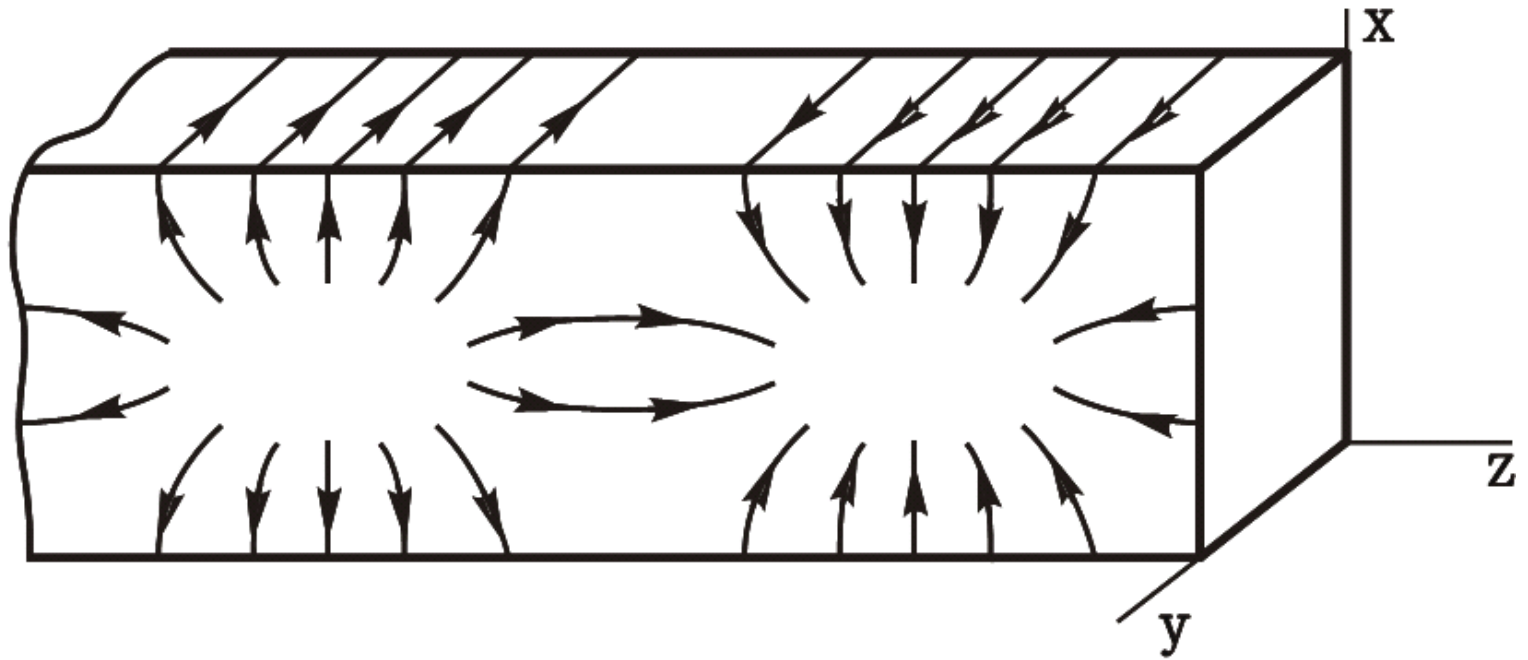
$$H_z = H_0 \cos\left(\frac{\pi}{a}x\right) e^{ik_z z}$$

4. bE_{10} wave electromagnetic field



4-9
y

4. E_{10} wave electromagnetic field



4-10
y