

Experimental equation of state in pp and p \bar{p} collisions and phase transition to quark gluon plasma

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Abstract

We deduce approximate equations of state from experimental measurements in pp and p \bar{p} collisions. Thermodynamic quantities are estimated combining the measure of average transverse momentum $\langle p_T \rangle$ vs pseudorapidity density $\frac{dN_{ch}}{d\eta}$ with the estimation of the interaction region size from measures of Bose Einstein correlation, or from a theoretical model which relates $\frac{dN_{ch}}{d\eta}$ to the impact parameter. The results are very similar to theory predictions in case of crossover from hadron gas to quark gluon plasma. According to our analysis, the possible crossover should start at $\frac{dN_{ch}}{d\eta} \simeq 6$ and end at $\frac{dN_{ch}}{d\eta} \simeq 24$.

Keywords:

quark gluon plasma, average transverse momentum vs pseudorapidity density, equation of state, Bose Einstein correlation, hadron gas, sound velocity

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1. Introduction

Some of the most important questions about the transition to the quark gluon plasma (QGP), a new state of matter with partonic degrees freedom, are not yet fully answered. Among them the location of phase boundaries between hadronic gas and the QGP. The results of lattice QCD simulations concerning the order of phase transition depend strongly on the number of quark flavors and on the quark masses. For vanishing baryon chemical potential $\mu_b = 0$, the nature of transition can be a genuine phase transition (first order or continuous), or just a rapid change (crossover) over a small temperature range [1]. Estimates of energy densities which can be achieved in ultra-relativistic pp or p \bar{p} collisions with high multiplicities suggest values sufficiently high for experimental formation of the QGP [2].

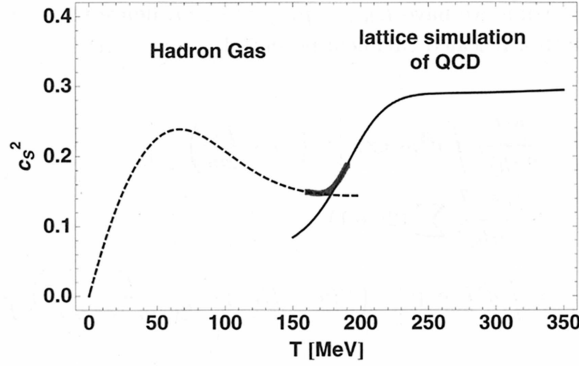
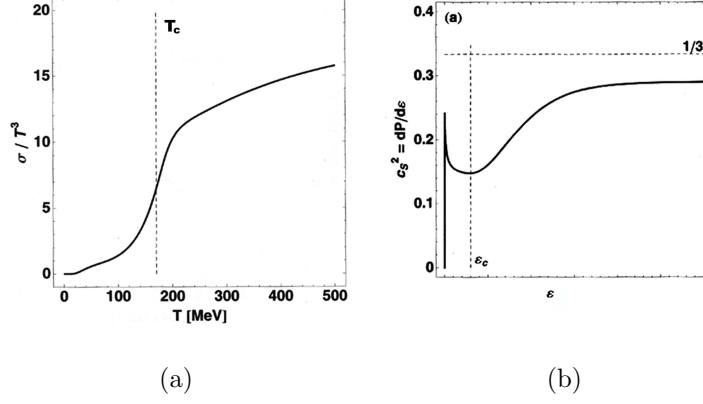
However it may be that, unlike what happens in heavy ion interactions, in pp and p \bar{p} the central blob of created matter never thermalizes [3], although there are different opinions [2, 4–7] which predict that thermodynamics concepts may be applied in pp or p \bar{p} high multiplicity events.

Probes of equation of state are among possible signatures of phase transition or crossover. The basic idea behind this class of signatures is the identification of modifications in the dependence of energy density ϵ , pressure P and entropy density σ of hadronic matter on temperature T . One wants to search for a rapid rise in the effective number of degrees of freedom, as expressed by the ratio ϵ/T^4 or σ/T^3 , over a small temperature range. One can expect a step-like rise as predicted by lattice simulations (Fig. 1), more or less steep depending from the presence of transition or crossover, and from the order of the transition in the former case. Finite volume effects may

26 cause important consequences for ϵ/T^4 and σ/T^3 : the latent heat and the
 27 jump in the entropy density are considerably reduced for small systems [8].
 28 Besides that, the critical temperature may shift to higher temperatures and
 29 the width of the transition may broaden for smaller volumes and there may
 30 be a smoothening of singularities due to the finite size of the system [8–10].

31 In 1982 it has been suggested by Van Hove [12] that an anomalous be-
 32 havior of average transverse momentum $\langle p_T \rangle$ as function of the multiplicity
 33 could be a signal for the occurrence of a phase transition in hadronic matter.
 34 His conjecture is based on the idea that the $\langle p_T \rangle$ distribution of secondaries
 35 reflects the temperature of the system and its evolution in the transverse
 36 direction, while the multiplicity per unit rapidity provides a measure of en-
 37 tropy [13, 14]. In a recent paper [15] one of us showed that from 22 to
 38 7000 GeV in 21 $\langle p_T \rangle$ vs pseudorapidity density $\frac{dN_{ch}}{d\eta}$ curves there is a slope
 39 change at $\frac{dN_{ch}}{d\eta} = 5.5 \pm 1.2$. Signals related to these slope changes may indi-
 40 cate transition to a new mechanism of particle production. Many years ago,
 41 in [16], we pointed out that pp at ISR and p \bar{p} data at CERN collider showed
 42 a kind of jump at $\frac{dN_{ch}}{d\eta} = 6$ and that it had to be investigated as a possible
 43 phase transition signal [17]. In 2002, Alexopoulos et al. [18] assumed that
 44 the system produced in p \bar{p} at $\sqrt{s} = 1800$ GeV for $\frac{dN_{ch}}{d\eta} > 6.75$ was above the
 45 deconfinement transition to explain their experimental results.

46 In present article, taking into account experimental results in pp and p \bar{p}
 47 at high energies [19–32], we show how measured physical quantities satisfy
 48 relations which, given proper approximations and correspondences, can give
 49 a representation of the equations of state (EOS) that describe the created
 50 system in the central region in pseudorapidity in high energy pp and p \bar{p}



(c)

Figure 1: Results of the lattice simulations of QCD for $T > T_c$ (critical temperature) and from ideal hadron-gas model for $T < T_c$.

1a: entropy density σ scaled by T^3 calculated in the hadron-gas model and by lattice simulations of QCD shown as function of temperature. The vertical line indicates the critical temperature.

1b: sound velocity c_s^2 shown as function of the energy density ϵ .

1c: temperature dependence of the square of the sound velocity at zero baryon density as function of T . In this case the critical temperature T is equal to 170 MeV.

From [11].

51 collisions. Starting from $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ experimental results together with the
52 estimation of the size S of the interaction area, which is obtained from the
53 measurements of the radii of emission in function of multiplicities [23–26],
54 or from a model which relates multiplicity to impact parameter [33], we
55 obtain relations among $\langle p_T \rangle$ and particle density σ_S , which seem to resemble
56 EOS curves predicted for hadronic matter with crossover to QGP. The $\langle p_T \rangle$
57 and S vs $\frac{dN_{ch}}{d\eta}$ relations contain the relevant information, which translates in
58 $\langle p_T \rangle$ vs σ_S correlations.

59 According to our knowledge, this is the first attempt to obtain an esti-
60 mation of the complete EOS for hadronic matter using experimental data
61 only.

62 2. Methods

63 The experimental results and the approximations made in this work are
64 the following.

65 2.1. $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$

66 As we mentioned before, $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ correlation at about $\frac{dN_{ch}}{d\eta} = 6$ shows
67 a slope change in all the experiments. In Van Hove scheme $\langle p_T \rangle$ reflects tem-
68 perature and the system evolution. On the other hand, the biggest part of
69 emitted particles is constituted by pions and the pion $\langle p_T \rangle$ is rather insensitive
70 to flow [34]. Thus, not identified charged particles $\langle p_T \rangle$ may be considered
71 as an estimation of the system temperature because it's not influenced very
72 much by a possible transverse expansion. Furthermore, transverse radius
73 R_{side} vs pair transverse momentum k_T in pp Bose Einstein correlation mea-
74 sures [24] show that, at least until $\frac{dN_{ch}}{d\eta} \simeq 3.4$, results are consistent with the

75 absence of transverse expansion, which further supports the adoption of $\langle p_T \rangle$
 76 as an identifier of temperature, because it's little affected by the expansion.

77 Since a substantial number of pions is the product of resonance decay
 78 and the particles originating from the resonance decays populate the low p_T
 79 region [11], in this work we consider mainly $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ correlations with
 80 a $p_{T \text{ min}}$ cut (> 400 MeV/c in CDF experiments Run I and Run II , > 500
 81 MeV/c in ALICE, and two different cuts, > 500 MeV/c and > 2500 MeV/c,
 82 in ATLAS experiment) in order to work with $\langle p_T \rangle$ values less influenced
 83 by this effect. Furthermore, diffractive events are substantially reduced for
 84 $\frac{dN_{ch}}{d\eta} \gtrsim 2$ in $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ plots with $p_{T \text{ min}} \geq 400$ MeV/c [21, 22].

85 We will show anyway also some results for $\langle p_T \rangle$ computed with $p_{T \text{ min}}$ cut
 86 0 and > 100 MeV/c. The structure of the relations we are going to show is
 87 still present in these measures.

88 In this work, $\langle p_T \rangle$ computed for different p_T cuts will be plotted without
 89 the application of corrections due to the cut in the used p_T range, apart
 90 from the case of events energy density estimation, in which we will use a
 91 corrected $\langle p_T \rangle$. Regarding $\frac{dN_{ch}}{d\eta}$, it is computed from the number of particle
 92 in a given region of pseudorapidity η and p_T , dividing by the amplitude of
 93 the η range and properly correcting for p_T cuts. In order to perform this last
 94 correction, we considered $\frac{dN_{ch}}{d\eta}$ curves for the different experiments, measured
 95 with and without p_T cuts, and multiplied by the ratio between correspondent
 96 values of $\frac{dN_{ch}}{d\eta}$ in the central region. All data are obtained from minimum
 97 bias experiments. For CDF run II 1960 GeV, high multiplicity trigger data
 98 are added to minimum bias data, for charged particle multiplicity $N_{ch} \geq 22$
 99 ($|\eta| < 1$, $p_T > 400$ MeV/c corresponding to $\frac{dN_{ch}}{d\eta}$ corrected ≥ 22) [15, 28].

100 Where available, we considered also raw data results (i.e. computed with-
 101 out experimental inefficiencies corrections) because the $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ plot and
 102 its derived plots are much sensible to experimental losses and, on the other
 103 hand, the application of corrections may involve some “smearing” of data
 104 which could highly modify the analyzed effects [19, 35]. For reasons of space
 105 we don’t show behaviors for raw data in this paper, because results are very
 106 similar to those for corrected data.

107 *2.2. Entropy Density Estimation*

The initial energy density in the rest system of a head-on collision has been argued to be [6]:

$$\epsilon \simeq \frac{\frac{dN_{ch}}{d\eta} \cdot \frac{3}{2} \langle p_T \rangle}{V}$$

V denotes the volume into which the energy is deposited. Similarly the initial entropy density is [2]:

$$\sigma \simeq \frac{\frac{dN_{ch}}{d\eta} \cdot \frac{3}{2}}{V}$$

108 As a result, ϵ is equal to $\sigma \cdot \langle p_T \rangle$. The volume V may be estimated as
 109 $V = S \cdot ct$, where S is the interaction area and ct is a longitudinal dimension
 110 we can traditionally consider to be about 1 fm long.

In order to study our system, we will use the quantity

$$\sigma_S = \frac{\frac{dN_{ch}}{d\eta} \cdot \frac{3}{2}}{S}$$

111 as an estimation of entropy density. In models like color glass condensate and
 112 percolation, the system physics depends on σ_S [36–38]. For the estimation of
 113 the area of interaction S , we proceed in different ways, our target being the
 114 obtainment of results which are robust respect to the definition of the area.

115 On the other hand, we are more interested in relations between variables
116 than in their absolute values.

117 *2.3. Bose Einstein correlation for emission region size estimation*

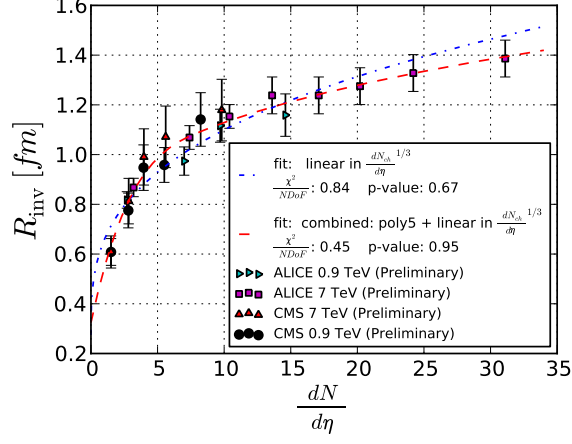
118 Using Bose Einstein correlation among emitted particles, measurements
119 of particle emission regions in many pp and p \bar{p} experiments have been done [23–
120 26, 31, 32, 39–41] In [23, 24], as already mentioned, the measurement of R_{side}
121 in function of k_T in pp, shows that the transverse radius doesn't depend on
122 k_T for low $\frac{dN_{ch}}{d\eta}$ values (< 3.4). This can be explained by the absence of ex-
123 pansion of the particle emission source, at least at these $\frac{dN_{ch}}{d\eta}$ values. For $\frac{dN_{ch}}{d\eta}$
124 values greater than 7, there is a dependence of R_{side} on k_T , so that probably
125 a source expansion is possible at least from this $\frac{dN_{ch}}{d\eta}$ value. It is thus possi-
126 ble that a new phenomenon is started in events with $\frac{dN_{ch}}{d\eta}$ between 3.4 and
127 7. The hypothesis of no expansion for low $\frac{dN_{ch}}{d\eta}$ values lets us approximate
128 the initial interaction section radius to be coincident to the final emission
129 radius. We take into account that for $\frac{dN_{ch}}{d\eta}$ values greater than about 7.5,
130 this approximation is more uncertain. Furthermore, resonance effects are
131 present, but, once more, we are not interested in the absolute values of the
132 interaction section, but in its behavior in function of $\frac{dN_{ch}}{d\eta}$. Not taking into
133 account these effects yields a systematic error on the value of the radius,
134 which we consider invariant for different values of $\frac{dN_{ch}}{d\eta}$. Given the similarity
135 in both the behavior and the absolute values of R_{side} and invariant radius
136 R_{inv} versus multiplicity, we use R_{inv} as an estimation of the interaction region
137 radius, mainly because R_{inv} data were measured for a larger $\frac{dN_{ch}}{d\eta}$ range than
138 R_{side} ones [23–26, 31, 32, 39, 40]. In Fig. 2, R_{inv} is shown as a function of
139 pseudorapidity density. In the left we only show data for CMS (preliminary)

140 and ALICE (preliminary) at $\langle k_T \rangle \simeq 0.35$, while in the right side we show
 141 the same results along data from other experiments (UA1, ABCDHW ISR,
 142 STAR). We fitted the data of Fig. 2a with two functional relations between
 143 R_{inv} and $\frac{dN_{ch}}{d\eta}$: the first is linear in the cube root of $\frac{dN_{ch}}{d\eta}$ [23, 24, 42] and the
 144 second is linear in cube root of $\frac{dN_{ch}}{d\eta}$ for $\frac{dN_{ch}}{d\eta} > 7.5$, matched with a 5th de-
 145 gree polynomial fit for smaller $\frac{dN_{ch}}{d\eta}$ values. The first fit gives a $\frac{\chi^2}{NDof} = 0.84$
 146 with p -value: 0.67, while the second gives a $\frac{\chi^2}{NDof} = 0.45$ with p -value: 0.95.
 147 Considering these results, we opted to use the second fit for the following
 148 analysis.

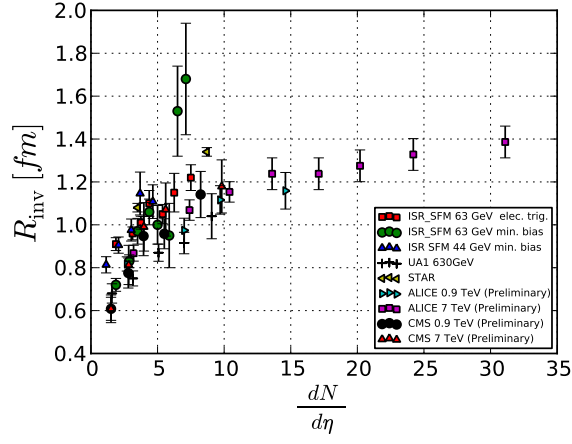
149 It has been stated that the behavior of radii in function of $\frac{dN_{ch}}{d\eta}$ doesn't
 150 depend on the experiment energy [41]. Data in Fig. 2 seem to confirm this
 151 statement, and justify our choice of a single relation for R_{inv} vs $\frac{dN_{ch}}{d\eta}$ for all
 152 energies.

153 In order to estimate the interaction region, we used the following alter-
 154 natives:

- 155 1. An area obtained using R_{inv} from the combined (polynomial + linear
 156 in cube root of $\frac{dN_{ch}}{d\eta}$) fit from Fig 2a. This choice may overestimate the
 157 interaction region in case of system expansion, being R_{inv} a measure of
 158 the emission region;
- 159 2. following ALICE results in R_{side} vs k_T , we make the hypothesis that
 160 no expansion is present in events with sufficiently low $\frac{dN_{ch}}{d\eta}$. So we
 161 use R_{inv} from the left (polynomial) part of the combined fit in Fig 2a,
 162 then we use a constant radius for $\frac{dN_{ch}}{d\eta} > 7.5$ as an estimation of the
 163 dimensions of the initial region before the possible expansion, making
 164 the assumption that at $\frac{dN_{ch}}{d\eta} \simeq 7.5$ the interaction region reaches its



(a)



(b)

Figure 2: R_{inv} vs $\frac{dN_{ch}}{d\eta}$ for different experiments [23–26, 31, 32, 40]. Left plot shows data from CMS (preliminary) and ALICE (preliminary) both at $\langle k_T \rangle \simeq 0.35$, along with linear fit in $\frac{dN_{ch}}{d\eta}^{1/3}$ and a combined fit: 5th degree polynomial for $\frac{dN_{ch}}{d\eta} < 7.5$ matched to linear fit in $\frac{dN_{ch}}{d\eta}^{1/3}$ for $\frac{dN_{ch}}{d\eta} > 7.5$. Right plot shows data from the first plot along with data from UA1, ABCDHW ISR, and STAR experiments.

165 maximum; at $\frac{dN_{ch}}{d\eta} = 7.5$ the R_{inv} value is 1.08 fm;

166 3. an area obtained from a model which relates the impact parameter to
167 the multiplicity of events [33].

168 From $\frac{dN_{ch}}{d\eta}$ values and from interaction areas, estimated as described
169 above, we obtained the values of density of particles for transverse area.

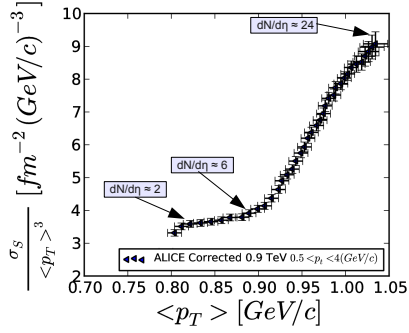
170 We considered the simplified case where the central blob volume V is the
171 same in all collisions for a given $\frac{dN_{ch}}{d\eta}$ [12]. We estimate an average σ from
172 the ratio between $\frac{dN_{ch}}{d\eta}$ and the estimated average V .

173 2.4. $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$

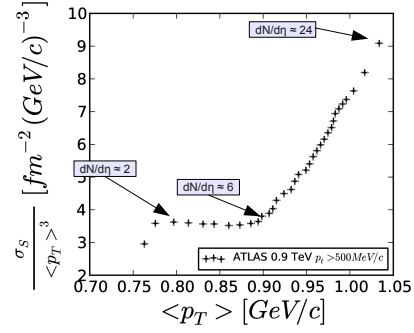
174 Using the estimated σ_S , the relation $\langle p_T \rangle$ vs σ_S can be studied. A slope
175 change in $\langle p_T \rangle$ vs σ_S plots is found at σ_S between 2.5 and 3 fm⁻², depending
176 on the method used for the estimation of area S and corresponds directly to
177 the slope change seen in $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ at $\frac{dN_{ch}}{d\eta} \simeq 6$.

178 Starting from σ_S and $\langle p_T \rangle$, we plotted $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$ curves, as an
179 experimental approximation of σ/T^3 vs T curves. See Figs. 3 and 4. We
180 obtained very similar $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$ curves from other pp and p \bar{p} experi-
181 ments [27, 29–31] (not shown).

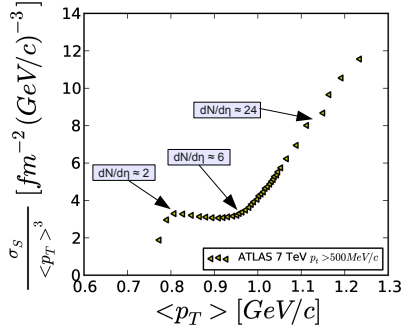
182 In figures, we put labels with corresponding $\frac{dN_{ch}}{d\eta}$ values for interesting
183 points, in order to relate these points to the characteristic values in $\frac{dN_{ch}}{d\eta}$.
184 In the different plots, different regions are recognizable. In particular, in all
185 plots we see that from the $\sigma_S/\langle p_T \rangle^3$ value corresponding to $\frac{dN_{ch}}{d\eta} \simeq 2$, up to
186 a value correspondent to $\frac{dN_{ch}}{d\eta} \simeq 6$, the curve is almost flat, then rises very
187 quickly. This behavior is similar to the one in σ/T^3 curve, in presence of
188 crossover, starting from a state of matter, identified by σ/T^3 nearly constant



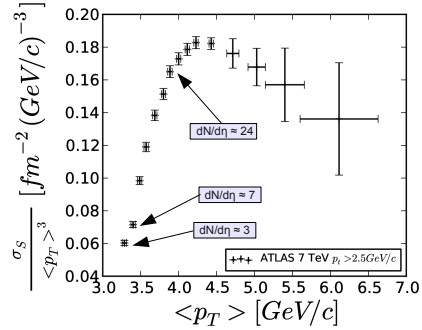
(a)



(b)



(c)



(d)

Figure 3: $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$ plots. Area S from “5th degree polynomial + constant after $\frac{dN_{ch}}{d\eta} > 7.5$ ” fit.

3a: ALICE at $\sqrt{s} = 0.9$ TeV, $0.5 < p_T < 4$ GeV/c, $|\eta| < 0.8$, Minimum Bias.

3b: ATLAS at $\sqrt{s} = 0.9$ TeV, $p_T > 0.5$ GeV/c, $|\eta| < 2.5$, Minimum Bias.

3c: ATLAS at $\sqrt{s} = 7$ TeV, $p_T > 0.5$ GeV/c, $|\eta| < 2.5$, Minimum Bias.

3d: ATLAS at $\sqrt{s} = 7$ TeV, $p_T > 2.5$ GeV/c, $|\eta| < 2.5$, Minimum Bias.

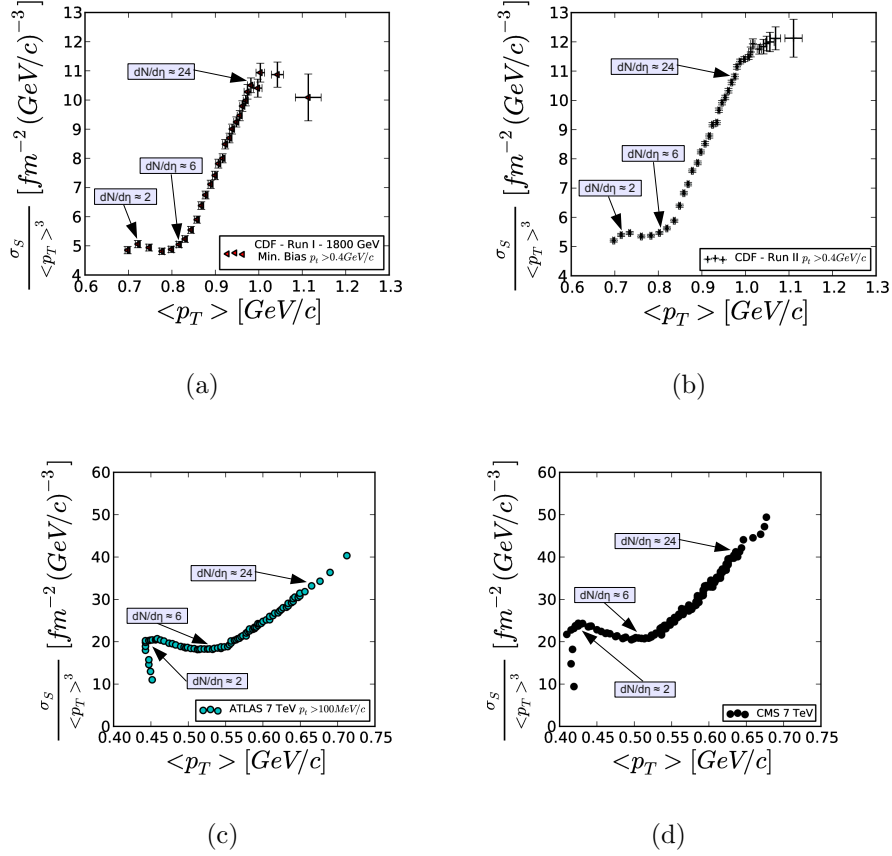


Figure 4: $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$ plots. Area S from “5th degree polynomial + constant after $\frac{dN_{ch}}{d\eta} > 7.5$ ” fit.

4a: CDF Run I at $\sqrt{s} = 1.8$ TeV, $p_T > 0.4$ GeV/c, $|\eta| < 1.0$, Minimum Bias.

4b: CDF Run II at $\sqrt{s} = 1.96$ TeV, $p_T > 0.4$ GeV/c, $|\eta| < 1.0$, Minimum Bias + High multiplicity trigger.

4c: ATLAS at $\sqrt{s} = 7$ TeV, $p_T > 0.1$ GeV/c, $|\eta| < 2.5$, Minimum Bias.

4d: CMS at $\sqrt{s} = 7$ TeV, $p_T > 0$ GeV/c, $|\eta| < 2.4$. Minimum Bias.

189 (region $2 \lesssim \frac{dN_{ch}}{d\eta} \lesssim 6$), and a crossover starting at $\frac{dN_{ch}}{d\eta} \simeq 6$ (Fig. 1). Besides,
 190 in plots with many points at high $\frac{dN_{ch}}{d\eta}$ values (ATLAS with $p_T > 2500$
 191 MeV/c, and CDF Run II 1960 GeV with $p_T > 400$ MeV), we observe a
 192 strong slope change around corresponding $\frac{dN_{ch}}{d\eta}$ values of about 24 or higher.
 193 It's worth noting that what seems to be a different behavior in the left side
 194 for ATLAS with $p_T > 2500$ MeV/c (Fig. 3d), is only due to the fact that all
 195 points correspond to $\frac{dN_{ch}}{d\eta} \gtrsim 7$, apart from the first point, which correspond
 196 to $\frac{dN_{ch}}{d\eta} \simeq 3.4$. The ratio between $\sigma_S/\langle p_T \rangle^3$ values corresponding to $\frac{dN_{ch}}{d\eta} \geq 24$
 197 and those corresponding to $\frac{dN_{ch}}{d\eta} \leq 6$ varies from 2 to 3, depending on the
 198 area calculation method used for the estimation of σ_S . This ratio in the case
 199 of EOS would correspond to the ratio between the number of the degrees of
 200 freedom of the state before and after the transition or the crossover. We note
 201 that for small size systems as it would be in the pp case, the jump in entropy
 202 density is considerably reduced [8–10] in comparison to the theoretical infinite
 203 volume case. In plots with $p_T > 100$ MeV/c (ATLAS 7 TeV) or $p_T > 0$ (CMS
 204 7 TeV), the first points have constant $\langle p_T \rangle$ with varying $\frac{dN_{ch}}{d\eta}$, which leads
 205 to an initial steep rise. After that, the curves assume the same behavior of
 206 previously seen plots.

207 2.5. Sound velocity c_s^2

208 One of the physical quantities used to characterize the state of a system is
 209 its squared sound velocity, defined as $c_s^2 = \frac{\sigma}{T} \cdot \frac{dT}{d\sigma}$, for constant V [11]. In our
 210 study, we approximate it with $c_s^2 = \frac{\sigma_S}{\langle p_T \rangle} \cdot \frac{d\langle p_T \rangle}{d\sigma_S}$. It is really interesting that
 211 if $\langle p_T \rangle$ is proportional to T and if σ_S is proportional to the entropy density,
 212 then the c_s^2 value obtained in this approximation is equal to the right value

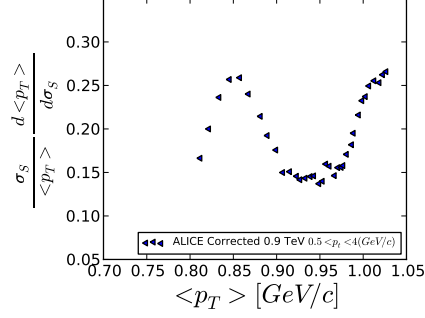
213 of $c_s^2 = \frac{\sigma}{T} \cdot \frac{dT}{d\sigma}$, because proportionality constants cancel out. In order to
 214 obtain our c_s^2 estimation, from $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ curves and from σ_S values, we
 215 compute the curve $\langle p_T \rangle$ vs σ_S , to which we apply numerical derivation. We
 216 cope with the statistical fluctuation in data points using a combination of
 217 Gaussian and Savitzky-Golay filters [43]. Examples of c_s^2 vs $\langle p_T \rangle$ curves are
 218 shown in Figs. 5a and 5c.

219 The so obtained c_s^2 estimation resembles the typical shape of a phase
 220 transition or a crossover: a descent, a minimum region and a following rise,
 221 as it's also obtained analytically from EOSs which present a phase transition
 222 or a crossover. The minimum value reached by the estimation of c_s^2 in the
 223 different experimental curves varies from 0.08 to 0.18 and could correspond
 224 to what it's called the EOS softest point [17].

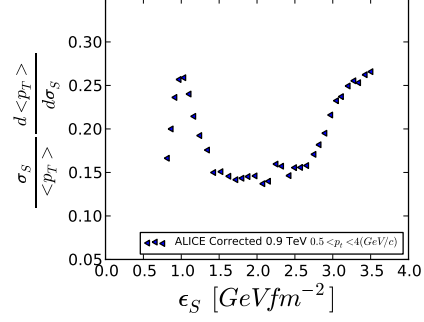
225 Recently Refs. [44–46] estimate c_s^2 minimum value for realistic EOS to
 226 be around 0.14. From $\epsilon_S \simeq \langle p_T \rangle \cdot \sigma_S$ we compute c_s^2 vs ϵ_S curves, that are
 227 approximations of c_s^2 vs energy density. We report these curves in Figs. 5b
 228 and 5d.

229 In this case, ϵ_S values are calculated using $\langle p_T \rangle$ values from $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$
 230 curves with no $p_{T \text{ min}}$ cut at corresponding energies, estimated in correspon-
 231 dence with the different $\frac{dN_{ch}}{d\eta}$ values. As Figs. 5 show, the numerical estima-
 232 tion of c_s^2 vs ϵ_S , is characterized by a maximum at low energy density fol-
 233 lowed by a minimum region, which is obtained for ϵ_S values in range 1.5 – 2.0
 234 GeV/fm², and a subsequent rise.

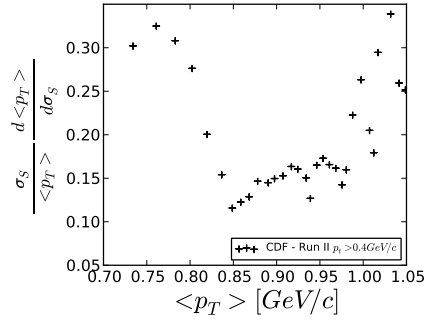
235 We note that ϵ_S as computed here is an estimation of the energy density
 236 for pseudorapidity unit and unit of transverse area. In order to estimate the
 237 volume energy density this should be divided by ct .



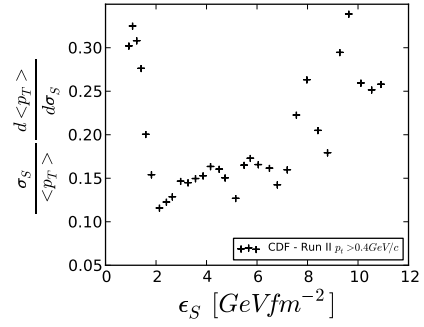
(a)



(b)



(c)



(d)

Figure 5: $c_s^2 = \frac{\sigma_S}{\langle p_T \rangle} \cdot \frac{d\langle p_T \rangle}{d\sigma_S}$ vs $\langle p_T \rangle$ or ϵ_S , using two different fits for area S estimation.

ALICE at $\sqrt{s} = 0.9$ TeV, $0.5 < p_T < 4$ GeV/c, $|\eta| < 0.8$, Minimum Bias; area S from “5th degree polynomial + linear in $\frac{dN_{ch}}{d\eta}^{1/3}$ after $\frac{dN_{ch}}{d\eta} > 7.5$ ” fit.

5a: c_s^2 vs $\langle p_T \rangle$, 5b: c_s^2 vs ϵ_S .

CDF Run II at $\sqrt{s} = 1.96$ TeV, $p_T > 0.4$ GeV/c, $|\eta| < 1.0$, Minimum Bias + High multiplicity trigger; area S from “5th degree polynomial + constant after $\frac{dN_{ch}}{d\eta} > 7.5$ ” fit.

5c: c_s^2 vs $\langle p_T \rangle$, 5d: c_s^2 vs ϵ_S .

238 **3. Discussion**

239 The shape of the $\sigma_S/\langle p_T \rangle^3$ approximation to the EOS is very similar,
 240 using both R_{inv} from the fit on all $\frac{dN_{ch}}{d\eta}$ space and R_{inv} fitted up to $\frac{dN_{ch}}{d\eta} =$
 241 7.5 and then maintained constant. It slightly varies when using the area
 242 from the impact parameter model, but the slope change at $\sigma_S/\langle p_T \rangle^3$ values
 243 corresponding to $\frac{dN_{ch}}{d\eta}$ around 6 is still present, as well as the change at
 244 $\sigma_S/\langle p_T \rangle^3$ values corresponding to $\frac{dN_{ch}}{d\eta}$ about 24.

245 In order to avoid possible systematics due to calculation involved in the
 246 area definition, we plotted directly $\frac{dN_{ch}}{d\eta}/\langle p_T \rangle^3$ vs $\langle p_T \rangle$: this is equivalent to
 247 obtain $\sigma_S/\langle p_T \rangle^3$ curves considering a transverse section which is constant for
 248 all $\frac{dN_{ch}}{d\eta}$ values. For space reason we don't show these plots in this paper.
 249 In this case the shape doesn't resemble an EOS shape anymore, but the
 250 slope changes at $\frac{dN_{ch}}{d\eta} \simeq 6$ and $\frac{dN_{ch}}{d\eta} \simeq 24$ are still present, because they are
 251 contained in the $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ correlation.

252 The shape of the curves obtained from experimental data ($\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$,
 253 c_s^2 vs $\langle p_T \rangle$ and c_s^2 vs energy) depends on experimental $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ curves and
 254 from the value of the area used to obtain density sigmas. Systematic errors
 255 in $\langle p_T \rangle$, $\frac{dN_{ch}}{d\eta}$, and R_{inv} measurements don't lead to appreciable variations in
 256 $\langle p_T \rangle$ vs σ_S behavior, which is what we are interested on.

257 It seems to us that the main result of this work is that putting together
 258 experimental data of $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ and R_{inv} vs $\frac{dN_{ch}}{d\eta}$, curves are obtained which
 259 are the reproduction of theoretical EOS curves.

260 Regarding model comparison, we obtained $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$ plots starting
 261 from Montecarlo curves (*Pythia ATLAS AMBT1* and *Pythia8* for ATLAS
 262 and CMS experiment respectively), which are shown in Fig. 6.

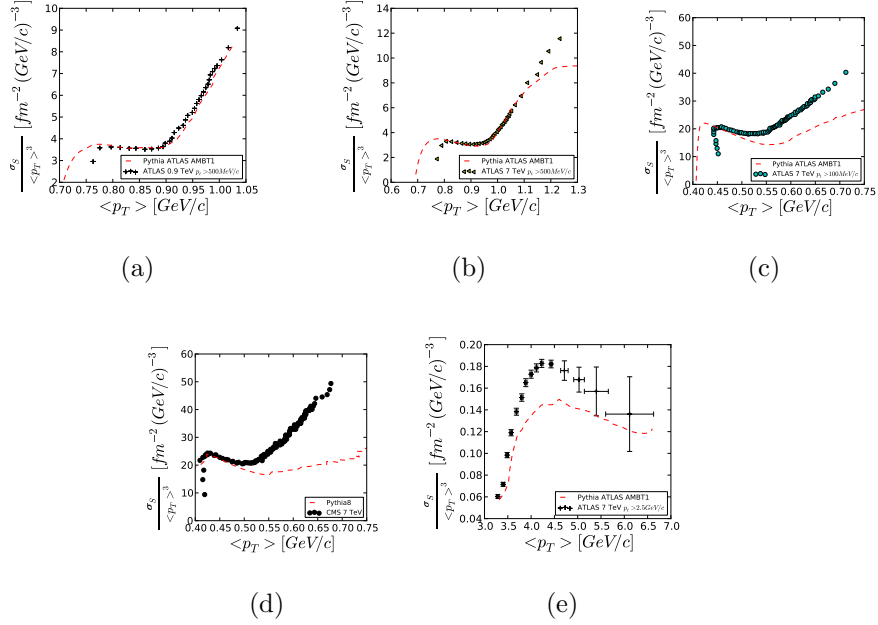


Figure 6: $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$. Comparison with models.

6a: ATLAS at $\sqrt{s} = 0.9$ TeV, $p_T > 0.5$ GeV/c, $|\eta| < 2.5$, Minimum Bias and *Pythia ATLAS AMBT1*.

6b: ATLAS at $\sqrt{s} = 7$ TeV, $p_T > 0.5$ GeV/c, $|\eta| < 2.5$, Minimum Bias and *Pythia ATLAS AMBT1*.

6c: ATLAS at $\sqrt{s} = 7$ TeV, $p_T > 0.1$ GeV/c, $|\eta| < 2.5$, Minimum Bias and *Pythia ATLAS AMBT1*.

6d: CMS at $\sqrt{s} = 7$ TeV, $p_T > 0$ GeV/c, $|\eta| < 2.4$, Minimum Bias and *Pythia8*.

6e: ATLAS at $\sqrt{s} = 7$ TeV, $p_T > 2.5$ GeV/c, $|\eta| < 2.5$, Minimum Bias and *Pythia ATLAS AMBT1*.

263 Some models on which tuning has been done, for example with CDF Run
 264 II data at 1960 GeV for $p_T > 400$ MeV/c, well reproduce the $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$
 265 curve at higher (7 TeV) or lower (0.9 TeV) energies with $p_T > 500$ MeV/c. It
 266 is clear that in these cases, starting from the $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ curves of models and
 267 using Bose Einstein correlation or the impact parameter–multiplicity relation
 268 for σ_S estimation, curves similar to the experimental ones are obtained. On
 269 the other hand, models don't predict well $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ curves with low p_T min,
 270 and consequently $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$ curves as shown for the comparison of
 271 models at 7 TeV for CMS and ATLAS data, respectively with $p_T > 0$ MeV/c
 272 and $p_T > 100$ MeV/c [20–22, 47].

273 The interpretation of curve shapes as experimental “estimation” of EOS
 274 depends on how much likely are the correspondences between $\langle p_T \rangle$ and T ,
 275 and between measured σ_S and entropy.

276 4. Conclusion

277 The result we consider to be the most important is the following: in
 278 many experiments [19–22, 27–31] from 31 GeV to 7000 GeV, starting from
 279 $\langle p_T \rangle$ vs $\frac{dN_{ch}}{d\eta}$ and using results from measures of radii with Bose Einstein
 280 correlation or from a model that relates impact parameter and multiplicity,
 281 we obtained that $\sigma_S/\langle p_T \rangle^3$ vs $\langle p_T \rangle$ and $c_s^2 = \frac{\sigma_S}{\langle p_T \rangle} \cdot \frac{d\langle p_T \rangle}{d\sigma_S}$ reproduce the shape
 282 of hadronic matter EOSs and squared sound velocity respectively, in presence
 283 of crossover or phase transition. From the plots, a neat change around $\frac{dN_{ch}}{d\eta}$
 284 around 6, where the crossover or the phase transition seems to start, and
 285 another possible change at $\frac{dN_{ch}}{d\eta}$ around 24 are observed. The curve c_s^2 vs ϵ_S
 286 has a minimum around a “transverse” energy density of about 1.5 GeV/fm².

287 In order to understand if these behaviors have a real physical meaning
288 or are just casual, results of measures in the following regions should be
289 compared: $2 \lesssim \frac{dN_{ch}}{d\eta} \lesssim 6$, $\frac{dN_{ch}}{d\eta} \gtrsim 6$, $6 \lesssim \frac{dN_{ch}}{d\eta} \lesssim 24$ and $\frac{dN_{ch}}{d\eta} \gtrsim 24$.

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