Galactic Phase Transition at $E_c = 0.11 \, eV$ from Rotation Curves of Cored LSB and nonperturbative Dark Matter Mass

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We analyze the a set of seventeen rotation curves of Low Surface Brightness (LSB) galaxies from the The HI Nearby Galaxy Survey (THINGS) with different mass models to study the core structure and to determine a phase transition energy scale (E_c) between hot and cold dark matter, due to nonperturbative effects in the Bound Dark Matter (BDM) model. Our results agree with previous ones implying the cored profiles are preferred over the N-body motivated cuspy Navarro-Frenk-White (NFW) profile. We find an average galactic core radius of $r_c = 260 \times 10^{\pm 1.3}$ pc and a phase transition energy $E_c = 0.11 \times 10^{\pm 0.46}$ eV, that is of the same order of magnitude as the sum of the neutrino masses.

Understanding the distribution of Introduction. dark matter (DM) in galaxies has been a major work in recent times [1, 2]. Late-type Low Surface Galaxies (LSB) galaxies are of special interest since it is believed that they are dominated by DM, and high resolution HI, H_{α} and optical data can help to distinguish among the different DM profiles proposed in the literature. There are essentially two types of halo profiles, the ones stemming from cosmological N-body simulations that have a cusp in its inner region, e.g. Navarro-Frenk-White (NFW) profile [3]. On the other hand, the phenomenological motivated cored profiles, such as the Burkert or Pseudo-Isothermal (ISO) profiles [4]. Cuspy and cored profiles can both be fitted to most LSB rotation curves, but with a marked preference for a cored inner region with constant density. Furthermore, cuspy profiles that do fit to galaxies in many cases suffer from a parameter inconsistency, since their concentrations (c) are too low and velocities V_{200} are too high in comparison to the ones expected from cosmological simulations [2, 5]. However, different systematics may play an important role in the observations such as noncircular motions, resolution of data and other issues [6, 7]. There are attempts to reconcile both approaches through evolution of DM halo profiles including baryonic processes [9] to transform cuspy to shallower profiles that follow the solid-body velocity curve $(v \sim r)$ observed in late-type LSB. However, this issue is a matter of recent debate [8].

Recently one of us proposed a new type of Dark Matter, called bound dark matter (BDM) [13], motivated by particle physics in which DM particles are relativistic at high energy densities, $\rho_{BDM} > \rho_c$ above the phase transition scale energy scale $\rho_c = E_c^4$, i.e. we have Hot DM (HDM) with peculiar velocity $v \simeq c$. But, for lower energy densities than ρ_c the BDM particles acquire a large mass due to nonperturbative physics and they behave as standard Cold DM (CDM) particles with $v \ll c$. The phase transition between CDM and HDM given by the scale $\rho_c \equiv E_c^4$ can be determined theoretically or phenomenologically by consistency with cosmological or galactic data. In the present work we will estimate its value through the study of the rotation curves of LSB galaxies.

The work here is twofold. On the one hand, we use galactic rotation curves to extract information on the possible core nature of DM dominated galaxies, and on the other, we determine the fundamental parameters behind our DM proposal. To perform these tasks we use four different halo mass profiles (NFW, BDM, Burkert, ISO) and five stellar mass models (Min.Disk, Min.Disk+gas, Kroupa, diet-Salpeter, Free Γ_*). However, given the amount of data, in the present work we limit ourselves to present the main results and special features of the study, referring to the most extensive work in [10]. For the analysis we use The HI Nearby Galaxy Survey (THINGS), which collects high resolution and excellent sensitivity of the velocity fields revealing extended measurements of gas rotation velocities and circular baryonic matter trajectories [11]. We will show that the LSB rotation curves yield a phase transition energy scale E_c , between HDM and CDM for our BDM profile, at $E_c = 0.11^{+0.21}_{-0.07}$ eV. This E_c is a new fundamental scale for DM and can also be theoretically determined using gauge group dynamics. However, even though we propose E_c as a new fundamental constant for DM it is important to notice that its value does depends on the choice of BDM profile used and on the quality of the observational data. The coincidence in the size of the sum of neutrino masses with the magnitude as E_c could open an interesting connection between the generation of DM and neutrinos masses.

BDM Model. Cosmological evolution of gauge groups, similar to QCD, have been studied to understand the nature of dark energy [16] and also DM [17]. For an asymptotically free gauge group the strength of the fundamental interaction increases with decreasing energy and the non-perturbative mechanism generates the mass of bound states, as baryons in QCD. In this case, the mass of the bound states particles is not the sum of its component particles but it is due to the binding energy and is parameterized by Λ_c . The condensation or phase transition scale is defined as the energy where the gauge

coupling constant g becomes strong, i.e. $g(\Lambda) \gg 1$, giving a condensation scale $\Lambda_c = \Lambda_i e^{-8\pi^2/bg_i^2}$, where b is the one-loop beta function which depends only on the number of fields in the gauge group (for example for a SUSY gauge group $SU(N_c), N_f$, where $N_c(N_f)$ is the number of colors (flavors), we have $b = 3N_c - N_f$) and g_i is the value of the coupling constant at an initial scale Λ_i . Clearly, Λ_c is exponentially suppressed compared to Λ_i and we can understand why Λ_c is much smaller then the initial Λ_i , which may be identified with the Planck, Inflation or Unification scale. The order of magnitude of the mass of these particles is $m_{BDM} = d E_c$ with $d = \mathcal{O}(1)$ a proportionality constant. In QCD one has $\Lambda_{QCD} \simeq 200 \,\text{MeV}$ with the pion (proton) mass $m_{\pi} \simeq 140 \text{ MeV} \ (m_b \simeq 939 \text{ MeV}), \text{ giving a propor-}$ tionality constant is in the range 0.7 < d < 5, with bound mass much larger than the mass of the quarks $(m_u \simeq (1-3) \text{ MeV}, m_d \simeq (3.5-6) \text{ MeV})$. In our case the gauge group and elementary fields are not part of the standard model (SM). Our dark gauge group is assumed to interact with the SM only through gravity and is widely predicted by extensions of the SM, such as brane or string theories. We can relate E_c to Λ_c since the energy density depends on the average energy per particle and the particle number density n, i.e. $\rho_c \equiv E_c^4 = \Lambda_c n$. There are two natural places where one may encounter high energy densities for dark matter. One is at early cosmological times and the second place is in galactic inner regions. Here we are interested in the latter case. Away from the center of the galaxies the energy density decreases and one has $\rho_{BDM} < \rho_c$. In this region the BDM particles are CDM. Since CDM is well parameterized by a cuspy NFW profile $\rho_{NFW} = \rho_0/[r/r_s(1+r/r_s)^2)]$ we expect BDM to have this limit away from the galactic center and as long as $\rho_{BDM} \ll \rho_c$. However, in the inner region the DM energy density increases and once ρ_{BDM} reaches ρ_c we have a phase transition and the BDM particles become relativistic with a dispersion velocity $v \simeq c$ and therefore forming a core inner region. At this stage the NFW profile would no longer describe the behavior of our BDM. Therefore, since our BDM behaves as CDM away from the galactic center but the density but has a core inner region the proposed BDM profile is [13]

$$\rho_{BDM} = \frac{\rho_0}{\left(\frac{r_c}{r_s} + \frac{r}{r_s}\right) \left(1 + \frac{r}{r_s}\right)^2},\tag{1}$$

which contains three parameters: a typical scale length (r_s) and density (ρ_0) of the halo, and a core radius (r_c) . The BDM profile coincides with ρ_{NFW} at large radius but has a core inner region, when the halo energy density ρ_{BDM} reaches the value $\rho_c = E_c^4$ at $r \simeq r_c$ with

$$\rho_c \equiv \rho_{BDM}(r = r_c) \simeq \rho_0 r_s / 2r_c. \tag{2}$$

The relevant parameters to determine the inner core structure of galaxies are the value of $E_c = \rho_c^{1/4}$ and r_c . The parameters ρ_0 and r_s depend on the initial conditions and formation of each galaxy. Analysis of LSB Galaxies. We limit our sample to

MINIMUM DISK								
			BDM	NFW				
Galaxy	r_s	$\log \rho_0$	r_c	E_c	χ^2_{red}	r_s	$\log \rho_0$	χ^2_{red}
DDO154	3.6	7.4	1.35	0.05	0.38	14.5	6.2	1.48
NGC2841	4.7	8.6	0.001	1.29	0.58	4.7	8.6	0.58
NGC3031	1.6	9.4	0.19	0.22	4.24	1.9	9.2	4.20
NGC3621	7.8	7.5	0.01	0.22	2.04	7.9	7.5	2.02
NGC4736	0.3	10.7	0.05	0.41	1.69	0.3	10.5	1.67
NGC6946	6.0	8.0	0.12	0.16	1.37	6.6	7.9	1.38
NGC7793	7.2	7.4	0.06	0.15	3.69	8.7	7.3	3.75
IC2574	17.3	7.0	18.28	0.04	0.43	$\sim 10^4$	2.9	6.17
NGC2366	2.3	8.0	2.25	0.03	2.11	18.6	6.2	4.45
NGC2903	1.9	9.3	1.90	0.08	1.72	3.9	8.4	2.36
NGC2976	2.5	8.5	2.53	0.09	0.69	$\sim 10^4$	3.3	2.86
NGC3198	3.8	8.4	3.76	0.10	0.59	9.0	7.4	1.80
NGC3521	2.0	9.3	2.00	0.08	1.37	5.3	8.2	7.17
NGC925	10.4	7.5	12.18	0.03	0.31	$\sim 10^4$	2.3	1.46

TABLE I: We compare the main BDM parameters $(r_s, \rho_0, r_c, \text{ and } E_c)$ with those of NFW (r_s, ρ_0) as well as the χ^2_{red} obtained from the fittings of our galaxy sample with $r_c \neq 0$. The galaxies are separated in Group A and B as explained in the main text. Scales distances (r_s, r_c) are given in kpc; the density ρ_0 in both profiles is given in M_{\odot}/kpc^3 , and the energy E_c in given in eV.

(early type and dwarf) THINGS galaxies with smooth, symmetric and extended-to-large-radii rotation curves. The set consists of seventeen low luminous LSB galaxies. These observations represents the best available data to study the DM mass distribution and it has been used in works concerning the core versus cusp discrepancy controversy [7]. For technical details and systematic effects see [11]. Our mass models include the three main components of a spiral galaxy: thin gaseous disk, V_{gas} , a thick stellar disk, V_{\star} , and a DM halo, V_{halo} . We have not considered a bulge because it is estimated to contain a small fraction of the total luminosity in our galaxy sample and therefore it has a small or null effect in the analysis. The gravitational potential of the galaxy is the sum of each mass component, thus the observed rotational velocity is $V_{obs}^2 = V_{halo}^2 + V_{gas}^2 + \Upsilon_{\star}V_{\star}^2$. Available photometry, extracted from the SINGS images at the 3.6 μm , shows that the stars in our sample of galaxies are distributed in a thin disk, with exponential central surface density profile $\Sigma(R) = \Sigma_0 e^{-R/R_d}$. When R_d is the scale length of the disk and Σ_0 is the central surface density with units $[M_{\odot} \text{pc}^{-2}]$. The rotation velocity of an exponential disk is given by the well know Freeman formula. The contribution of the gaseous disk is directly derived from the HI surface density distribution. The kinematics of stars brings a challenging problem in the analysis, mainly due to the uncertainty of the mass-to-light ratio (Υ_{\star}) , that is an additional constant, free parameter in the mass model. The stellar contribution to rotational curves is in many cases dominant close to the galactic center and this interferes with the determination of the core parameters. Some considerations has been made in order to reduce

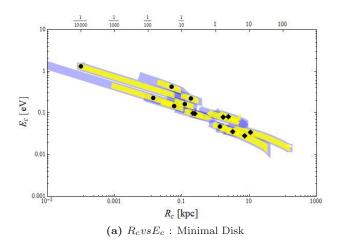


FIG. 1: We show the values of the cored r_c and energy E_c and its respectively confidence levels for the different Group A and Group B galaxies, giving $E_c \simeq 0.1 \text{ eV}$ and core radius $r_c \simeq 260 \text{ pc}$. The circles and diamonds represent each galaxies from G.A. and G.B. (inner), respectively. In both cases the areas in yellow (light) and blue (dark) represent the σ and 2σ confidence levels.

this uncertainty in the parameters [18], but still the stellar contribution is not well known and depends on extinction, star formation history, initial mass function (IMF), among other issues. We present a disk-halo decomposition using different assumptions for the stellar Υ_{\star} : i) DM alone (Min.Disk); ii) DM and gas (Min.Disk+gas); iii) Kroupa, consider as the minimal limit for the stellar disk; iv) diet-Salpeter, stellar population synthesis model yields a maximum stellar disk; and v) Free Υ_{\star} , treat the mass-to-light ratio as an extra free parameter in the model.

We have analyzed the rotation curves of seventeen galaxies using the above-mentioned five disk models and four different DM profiles (BDM, NFW, Burkert, ISO). Since we have a large number of data, and because we want to emphasize the main results, here we present the general conclusions and we show results for the Min.Disk scenario for BDM and NFW, only. However, a full comparison and a detailed analysis between all the different profiles and mass models can be found in [10]. We also perform 1 and 2 σ likelihood contour plots for the BDM parameters, r_c and ρ_0 for the different galaxies and mass models [10]. We have grouped the galaxies into three blocks according to the ratio r_c/r_s of the central fitted value for the min.disk scenario. The first group (G.A.) has a fitted $r_c/r_s < 1$, the second group (G.B.) has $r_c/r_s \simeq 1$, and finally, the third group (G.C.) has $r_c/r_s < 10^{-6}$. We shall explain the physical interpretation of the results for each group in the following paragraphs. Since the energy E_c and r_c can take values $(0,\infty)$ the correct distribution for the sample that we considered is the log-normal distribution, which is used to compute the statistics for the different BDM parameters. We obtain seven galaxies (Group A) with fitted values $r_s > r_c \neq 0$ that are shown in Table I. For these galaxies we obtain average values

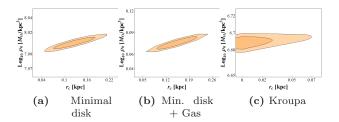


FIG. 2: We display the 2D contour plots for the BDM parameters ρ_0 and r_c for the galaxy NGC 6946. The two regions in each figure correspond to 1σ and 2σ confidence levels. Columns from left to right correspond to Min.Disk, Min.Disk+Gas, and Kroupa.

			ρ_{in}	ρ_{α}		
Galaxy	R_{max}	r_c	$\log \rho_0$	r_s	$\log \rho_0$	α
IC 2574	3.9	3.27	4.40	1347.58	6.77	0
NGC 2366	2.27	7.40	7.81	3.80	7.45	0.08
NGC 2903	4.5	1.70	8.01	6.60	8.4	0.52
NGC 2976	0.97	0.25	5.38	569.39	7.95	0.84
NGC 3198	6.82	0.21	6.89	16.64	8.02	0.9
NGC 3521	3.73	2.42	8.38	5.58	8.54	0.24
NGC 925	6.02	10.79	6.91	24.61	7.25	0.21

TABLE II: It is shown the BDM parameters and the slope α obtained from the fittings of the inner galactic region with the ρ_{in} and ρ_{α} profiles. The maximum distance (R_{max}) until which we consider the observation is given in kpc.

for: the core $r_c \simeq 40$ pc, $r_s \sim 5$ kpc, and the energy $E_c \simeq 0.11 \text{ eV}$ for the min.disk analysis, that are typical values for a galaxy, except for DDO 154 which has a larger core, $r_c = 1.35$ kpc. We notice that for all these galaxies, and predominantly when $r_c \ge 200 \text{ pc}$, BDM is clearly better than NFW. When comparing the BDM profile with the other two cored profiles, Burkert and ISO (Ref. [10]) we conclude that BDM is still better. In particular, Burkert and ISO profiles have difficulties when fitting a couple galaxies (NGC4736, NGC 3621) having $\chi^2_{red} > 5$ while BDM and NFW each have $\chi^2_{red} \le 2$. In the second case, Group B, we get a fitted value of $r_c \simeq r_s$ and BDM profile fits much better than NFW. In fact, the NFW profile in some cases over-predicts the velocity in the inner parts of the galaxy or does fit with unphysical values for $r_s > \mathcal{O}(10^4)$ or $\rho_0 < \mathcal{O}(10^3) M_{\odot}/\text{kpc}^3$, see Table I. The BDM profile gives $r_c \simeq r_s$ for all stellar mass models, having an average r_c value of ~ 6 and ~ 5 kpc for Min.Disk and Min.Disk+Gas, respectively. Since $r_c \simeq r_s$ with a large value this implies that our BDM profile is of the type $\rho \propto (r_c + r)^{-3}$ and having a strong core behavior. For this set of galaxies the Burkert and ISO profiles, as well as the BDM, fit much better than NFW, indicating that a core is needed. The BDM and Burkert profiles are slightly better than ISO when we consider Min.Disk and Min.Disk+Gas analysis. Otherwise, for Kroupa and diet-Salpeter mass models the BDM and ISO profile have equivalent χ^2_{red} and fit slightly better

than Burkert. To study in more detail the central region of the galaxies, we performed an analysis of the inner galactic region [10]. We define the inner region as the set of data for each galaxy with a constant slope value for the observed velocity, and for radius smaller than the fitted r_s in table I, and before the slope of v starts to decrease [10]. We computed the core radius, the central energy density, and the inner slope of the profile by examining the central region data with two different approaches: i) The first one by taking the limit $r \ll r_s$ in the BDM profile which gives $\rho_{in} = \rho_0 r_s (r_c + r)^{-1}$, ii) The second is with the ansatz profile $\rho_\alpha = \rho_0 r^{-\alpha}$, where α is the slope $\alpha \equiv -d \log[\rho] / \log[r]$. Both approaches are related by the equation $0 \leq \alpha = r/(r_c + r) < 1$, from which we obtained different values for α depending on the analyzed region, i.e. the slope in BDM takes the values $\alpha = (0, 1/2, 1)$ for $r = (0, r_c, r_c \ll r \ll r_s)$. In both approaches a core region is preferred and with a slope value in the interval $0 < \alpha < 0.52$ for most of the galaxies and a maximum slope of $\alpha \sim 0.84$, that implies that one is in the core dominant region, with $r/r_c = \alpha/(1-\alpha)$, or at most in the transition region between r_c and r_s . We also obtain that in case i) the length of the core radius is reduced, the average $r_c = 1.8$ kpc with energy $E_c \sim 0.06$ eV for min.disk scenario.

We only present here the conclusions of the last group C, composed of only three galaxies (NGC2403,NGC50455 and NGC7331) [10]. These galaxies have fitted values such that $r_c/r_s < 10^{-6}$ for most stellar mass models. The reduced number of data close to galactic center prevents us from finding whether these galaxies actually have or not a core. We conclude in [10] that ISO and Burkert are poorly fitting profiles, meanwhile BDM has a central value for $r_c \rightarrow 0$, so BDM reduces to NFW profile and both have equivalent fits. By applying inner analysis for these galaxies we obtain $0 \leq r_c \leq 50$ pc as a plausible interval that can fit the observations within the 2 σ error, although a more definitive conclusion would demand more data close to the center in these galaxies.

We have also calculated the 1 and 2 σ likelihood contour plots of r_c and ρ_0 for the different galaxies and mass models, but due to lack of space here we refer to [10]. In general we found that when more mass components are included in the analysis the confidence level area becomes broader and in some cases the confidence levels increase up to an order of magnitude for the r_c value [10]. Though r_c is different for each disk mass model there is an interval of values where r_c is consistent with all mass models within the 2 σ errors. We also obtained that in the Free Υ_{\star} scenario, the fitted value never gets a greater value than diet-Salpeter, which is consistent with [7]. We show in Fig. 1 the 1 and 2 σ contour plots of E_c vs r_c and for the Min.Disk case but we show in Table III the average for the different galaxies and mass models and we have a detailed analysis for each galaxy in [10]. We conclude that when more mass components are taking into account, mainly when the contribution of the stellar disk has a dominant behavior close to the galactic center, the

evidence of the core fades away. We also obtained that even if r_c is different for each mass model its value lays inside the confidence levels obtained from the other mass models for the same galaxy.

Energy Phase Transition E_c **.** The values of the core

BDM Statistics										
	Energy E_c				Core r_c					
Mass Models	\tilde{E}_{cn}	E_{c}	\hat{E}_c	E_{c_+}	σ_{E_c}	\tilde{r}_{cn}	r_{c}	\hat{r}_c	r_{c_+}	σ_{rc}
Min.Disk	0.14	0.04	0.11	0.33	0.46	1.91	0.01	0.26	5.41	1.31
M.Disk+gas										
						6.92				
diet-Salpeter	0.03	0.02	0.03	0.05	0.24	18.08	3.22	12.27	46.68	0.58

TABLE III: We show the statistics of the transition energy E_c and the core r_c for the BDM profile for the different mass models. In Columns (2) we show the arithmetic mean energy transition from HDM to CDM, E_{cn} . In column (3-5) we present the median energy \hat{E}_c and $E_{c\pm} \equiv \hat{E}_c 10^{\pm\sigma}$ assuming a log-normal distribution. In columns (6-9) we present the same statistics for the core distance r_c . The energy E_c and the core distance are given in unit of eV and kpc, respectively.

radius r_c and the transition energy $E_c = \rho_c^{1/4}$ are shown in Table I. In Fig. 1 we plot E_c vs r_c obtained from the minimal disk analysis with its respectively contour errors. The circles and diamonds represent each galaxies from Group A and Group B, respectively. The energy of transition between HDM and CDM takes place in Min.Disk mass model at energies and core radius up to 1 σ c.l. :

$$E_c = 0.11 \times 10^{\pm 0.46} \text{ eV}, \quad r_c = 260 \times 10^{\pm 1.31} \text{ pc} \quad (3)$$

The figures of E_c vs r_c for the other mass models (Min.Disk+Gas, Kroupa, and diet-Salpeter mass models) are included in [10]. Notice that the dispersion on E_c is much smaller than that of r_c and this is consistent with our BDM model since E_c is a new fundamental scale for DM model. Even though we propose E_c as a new fundamental constant for DM it is important to stress that its value depends on the choice of BDM profile and on high resolution data for the rotation curves. We can also theoretically estimate the value of E_c and Λ_c which are related via $\rho_c \equiv E_c^4 = \Lambda_c n$. We can then extract information from the underlying gauge group using gauge group dynamics. Using $\Lambda_c = \Lambda_i e^{-8\pi/bg_i^2}$ with $\Lambda_c \simeq E_c = 0.1$ eV and $g_i^2 = 1/2$ the gauge coupling at unification or inflation scale $\Lambda_i = 10^{16}$ GeV. We obtain $b = 8\pi/(g_i^2 Log[\Lambda_i/\Lambda_c]) \simeq 1$ and using that for a SUSY gauge group one has $b = 3N_c - N_f$ we could have for example a gauge group $SU(N_c = 3)$ with $N_f = 8$ fundamental particles. The energy transition in Eq.(3) is similar to the mean energy of a relativistic neutrino which is such that $\sum m_{\nu} < 0.58 \text{ eV}(95\% \text{ CL})$ if one assumes 3.04 neutrino species with degenerate mass eigenstates. Furthermore, an interesting connection could be further explored between the phase transition scale E_c of our BDM model, which also sets the mass of the BDM particles, to the neutrino mass generation mechanism [14].

However, we would like to emphasize that our BDM are not neutrinos, since neutrinos are HDM, and a combination of CDM plus neutrinos would have a cuspy NFW profile with CDM dominating in the inner region of the galaxies, assuming that CDM do indeed have a NFW profile as suggested by N-body simulation. [3]. A main difference between neutrinos and BDM is that neutrinos were in thermal equilibrium at $E \gg \text{MeV}$ with the standard model (SM) particles but BDM may not have been in thermal equilibrium with SM, as for example axion fields which are CDM but have a small mass m < eV. Conclusions. To summarize, we have tested different DM profiles with several mass models using LSB THINGS galaxies. The study favors BDM (core profiles) over the cuspy NFW, in accordance to general results found in other works [2, 7]. We presented here the analysis with Min.Disk for BDM and NFW profiles, but we have performed the study using the five different disk mass components for the BDM, NFW, Burkert, and Pseudo-Isothermal profiles [10]. We performed an analysis of the inner regions of Group B and C galaxies showing the ability to extract information from the rotation curves and the results are consistent with a core profile and we compute the core radius, central density and inner slope corresponding to the core region. In the cases where $r_c/r_s < 10^{-6}$ the BDM is indistinguishable from NFW profile and much better than Burkert or ISO profiles. The likelihood contour plots reveal how the central contribution of the stellar disk fades away the evidence of the core making $r_c \rightarrow 0$. The observational resolution of the THINGS sample is of high quality, but one still needs data closer to the center of some galaxies, on scales smaller than 200 pc, in order to discern between cored or cuspy profiles. This is because stars pose a very challenging problem when testing the core-cusp problem, largely due to the uncertainty of the mass-to-light ratio

and their dominant behavior close to the center of the galaxy.

We computed the 1 and 2 σ confidence levels for the BDM parameters E_c and r_c for the different galaxies and mass models. The contours plots show consistency in the fitted values of E_c and r_c for the different mass models for each galaxy. We found that the energy of transition between HDM and CDM takes places in Min.Disk mass models with an average energy $E_c = 0.11^{+0.21}_{-0.07}$ eV and with a core radius $r_c \sim 260 \times 10^{\pm 1.31}$ pc. Confidence level contours show that the core radius depends on the number of disk mass components taking into account in the analysis. We found that r_c is highly constrained if the stellar disk has a dominant behavior close to the center of the galaxy. However, we notice that even though r_c is different for each disk mass model there is an interval of values where r_{c} is consistent for all mass models within the 2 σ errors. The dispersion on E_c is much smaller than that of r_c and this is consistent with our BDM model since E_c is a new fundamental scale for DM model while r_c depends on r_s, ρ_0 which depends on the formation and initial conditions for each galaxy. Given the richer structure that the BDM profile has, through its transition from CDM to HDM (when $\rho \simeq \rho_c$), and it allows for a more physical explanation of the rotation curves of the different galaxies.

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