Research Article

Current-Mode Third-Order Quadrature Oscillator Using CDTAs

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This paper describes a current-mode third-order quadrature oscillator based on current differencing transconductance amplifiers (CDTAs). Outputs of two current-mode sinusoids with 90° phase difference are available in the quadrature oscillator circuit. The oscillation condition and oscillation frequency are orthogonal controllable. The proposed circuit employs only grounded capacitors and is ideal for integration. Simulation results are included to confirm the theoretical analysis.

1. Introduction

Various new current-mode active building blocks have received considerable attentions owing to their larger dynamic range and wider bandwidth with respect to operational amplifier-based circuits. As a result, current-mode active components have been increasingly used to realize active filters, sinusoidal oscillators, and immittances.

Quadrature oscillator is used because the circuit provides two sinusoids with 90° phase difference, as, for example, in telecommunications for quadrature mixers and single-sideband generators or for measurement purposes in vector generators or selective voltmeters. Therefore, quadrature oscillators constitute an important unit in many communication and instrumentation systems [1–17]. Two-integrator loop technique was developed to realize quadrature oscillators by using operational amplifiers or transconductance elements in [1, 2]. Holzel [3] proposed a method for realizing quadrature oscillator consists of two allpass filters and an inverter using operational amplifiers. Keskin et al. [15, 17] proposed two quadrature oscillators that were designed out by the method in [3] using current differencing buffered amplifiers (CDBAs) or current differencing transconductance amplifiers (CDTAs). Ahmed et al. [4] proposed two quadrature oscillator circuits that were realized base on the allpass filters and the noninverting integrators as building blocks using operational transconductance amplifiers (OTAs). This method was also used

in [16] to obtain a quadrature oscillator using CDBAs. Soliman [6] describes several quadrature oscillator circuits based on the modification of two-integrator loop technique using current conveyors. Because the high-order network has high accuracy and high-quality factor, it gives good frequency response with low distortion [9–12]. Prommee and Dejhan [9] proposed two third-order quadrature oscillators using OTAs. Horng et al. [10, 11] proposed four voltage-mode third-order quadrature oscillator circuits; each circuit uses three second-generation current conveyors (CCIIs). Maheshwari and Khan [12] proposed a current-mode third-order quadrature oscillator using four CCIIs.

In 2003, a new current-mode active element that is called current differencing transconductance amplifier (CDTA) was introduced [18]. Owing to the current conveying property, the CDTA is one of the modifications of the current conveyor (CC). Many applications in the design of active filter [19] and multiphase sinusoidal oscillator [20] using CDTAs as active elements have received considerable attention. A second-order current-mode quadrature oscillator consists of two CDTAs, four resistors, and two capacitors was presented in [17]. However, the capacitors used in this circuit are connected to the input terminals of the CDTAs. Since the input terminals of CDTA have parasitic resistances [20], this quadrature oscillator is not ideal for high-frequency applications. In 2006, Biolek et al. proposed a second-order current-mode quadrature oscillator based on
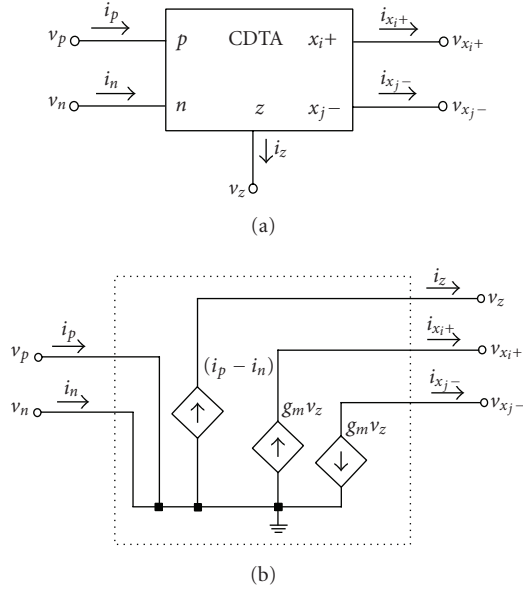
(a)

(b)

FIGURE 1: (a) Circuit symbol of CDTA. (b) Equivalent circuit of CDTA.

two-integrator loop technique [21]. The main disadvantage of this oscillator is that there is no control on the condition of oscillation.

In this paper, a CDTAs-based current-mode third-order quadrature oscillator circuit is presented. The oscillation condition and oscillation frequency of the proposed quadrature oscillator are orthogonal controllable. The proposed quadrature oscillator uses only grounded capacitors. The use of only grounded capacitors is especially interest from the fabrication point of view [22].

2. Proposed Circuit

The circuit symbol and the equivalent circuit of the CDTA are shown in Figure 1. The terminal characteristic of the CDTA can be described by the following equations [18]:

$$v_p = v_n = 0, \qquad i_z = i_p - i_n, \qquad i_x = \pm g_m v_z = g_m Z_z i_z, \tag{1}$$

where p and n are input terminals, z and $x\pm$ are output terminals, g_m is the transconductance gain, and Z_z is external impedance connected at the z terminal. According to the above equation and equivalent circuit of Figure 1(b), the current flowing out of the terminal $z(i_z)$ is a difference between the currents through the terminals p and n $(i_p - i_n)$. The voltage drop at the terminal z is transferred to the currents at the terminal x_i+ by the transconductance gain (g_m), which is electrically controllable by an external bias voltage. These currents that are copied to a general number of output current terminals x_j- are equal in magnitude but flow in opposite directions. A possible CMOS-based CDTA circuit realization is given in Figure 2 [17].

The CDTAs-based third-order quadrature oscillator is shown in Figure 3. The characteristic equation of the circuit in Figure 3 can be expressed as

$$s^3 C_1 C_2 C_3 + s^2 C_3 (C_1 g_{m2} + C_2 g_{m1}) + s C_3 g_{m1} g_{m2} + g_{m1} g_{m2} g_{m3} = 0. \tag{2}$$

The oscillation condition and oscillation frequency can be obtained as

$$g_{m3} = \frac{C_3 (C_1 g_{m2} + C_2 g_{m1})}{C_1 C_2}, \tag{3}$$

$$\omega_o = \sqrt{\frac{g_{m1} g_{m2}}{C_1 C_2}}. \tag{4}$$

From (3) and (4), the oscillation frequency can be controlled by g_{m1} or g_{m2}. The oscillation condition can be independently controlled by g_{m3}. From Figure 3, the current transfer function from I_{o2} to I_{o1} is

$$\frac{I_{o2}(s)}{I_{o1}(s)} = -\frac{g_{m3}}{sC_3}. \tag{5}$$

Under sinusoidal steady state, (5) becomes

$$\frac{I_{o2}(j\omega)}{I_{o1}(j\omega)} = \frac{g_{m3}}{\omega C_3} e^{j90^\circ}. \tag{6}$$

The phase difference, ϕ, between I_{o2} and I_{o1} is

$$\phi = 90^\circ \tag{7}$$

ensuring the voltages I_{o2} and I_{o1} to be in quadrature.

The proposed quadrature oscillator employs only grounded capacitors. The use of grounded capacitors is particularly attractive for integrated circuit implementation [22]. From (6), the magnitude of I_{o2} and I_{o1} need not the same. For the applications need equal magnitude quadrature outputs, another amplifying circuits are needed.

3. Nonideal Effects

Taking the nonidealities of the CDTA into account, Figure 4 shows the simplified equivalent circuit that is used to represent the nonideal CDTA [20]. In the figure, $\alpha_p = 1 - \varepsilon_p$ and ε_p ($|\varepsilon_p| \ll 1$) is the current tracking error from the p terminal to the z terminal of the CDTA, $\alpha_n = 1 - \varepsilon_n$ and $\varepsilon_n (|\varepsilon_n| \ll 1)$ is the current tracking error from the n terminal to the z terminal of the CDTA, and $\beta = 1 - \varepsilon_i$ and $\varepsilon_i (|\varepsilon_i| \ll 1)$ is the output transconductance tracking error from the z terminal to x terminal of the CDTA. Moreover, there are parasitic resistances (R_p and R_n) at terminals p and n and parasitic resistances and capacitances (R_z, C_z and R_x, C_x) from terminals z and x to ground. Reanalysing of the proposed quadrature oscillator in Figure 3 using the nonideal CDTA model and assuming that the operation oscillation frequencies, ω, are very much smaller than $1/C_x R_n$ or $1/C_x R_p$ and the parasitic resistances at the x terminals are very much greater than the parasitic resistances at p or n terminals of CDTAs, the characteristic equation of Figure 3 becomes
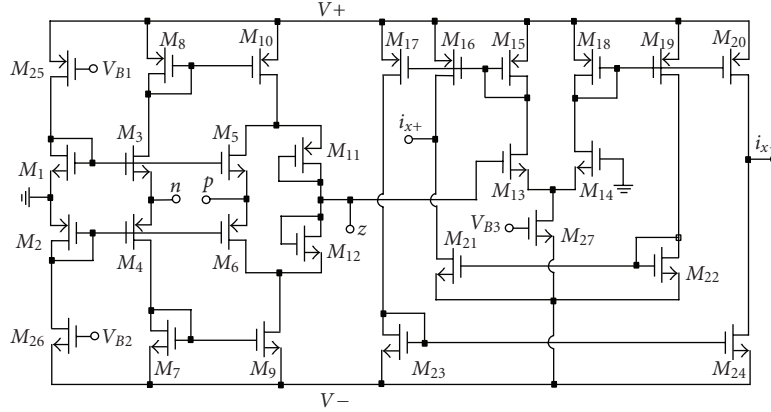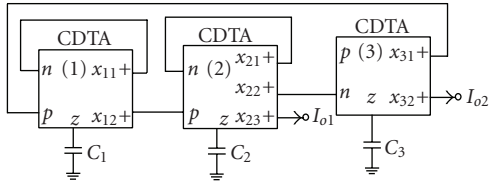
Figure 2: CMOS-based CDTA.

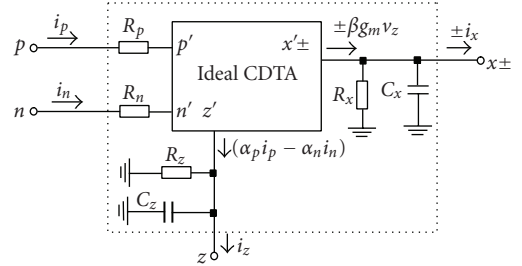Figure 3: The proposed current-mode quadrature oscillator.

$$s^3 C_1' C_2' C_3' + s^2 \big[C_1' C_3' (g_{m2}\alpha_{n2}\beta_{21} + G_{z2})$$
$$+ C_2' C_3' (g_{m1}\alpha_{n1}\beta_{11} + G_{z1}) + C_1' C_2' G_{z3} \big]$$
$$+ s \big[C_3' (g_{m1}g_{m2}\alpha_{n1}\alpha_{n2}\beta_{11}\beta_{21} + g_{m1}G_{z2}\alpha_{n1}\beta_{11}$$
$$+ g_{m2}G_{z1}\alpha_{n2}\beta_{21} + G_{z1}G_{z2})$$
$$+ C_1' (g_{m2}G_{z3}\alpha_{n2}\beta_{21} + G_{z2}G_{z3})$$
$$+ C_2' (g_{m1}G_{z3}\alpha_{n1}\beta_{11} + G_{z1}G_{z3}) \big]$$
$$+ g_{m1}g_{m2} \big(g_{m3}\alpha_{p1}\alpha_{p2}\alpha_{n3}\beta_{12}\beta_{22}\beta_{31} + G_{z3}\alpha_{n1}\alpha_{n2}\beta_{11}\beta_{21} \big)$$
$$+ G_{z3}(g_{m1}G_{z2}\alpha_{n1}\beta_{11} + g_{m2}G_{z1}\alpha_{n2}\beta_{21} + G_{z1}G_{z2}) = 0, \tag{8}$$

where $C_1' = C_1 + C_{z1}$, $C_2' = C_2 + C_{z2}$, $C_3' = C_3 + C_{z3}$.

The modified oscillation condition and oscillation frequency are

$$\frac{g_{m1}g_{m2}\boldsymbol{\mathcal{A}} + G_{z3}\boldsymbol{\mathcal{B}}}{C_1' C_3' \boldsymbol{\mathcal{C}} + C_2' C_3' \boldsymbol{\mathcal{D}} + C_1' C_2' G_{z3}}$$
$$= \frac{C_3' \boldsymbol{\mathcal{E}} + C_1' \boldsymbol{\mathcal{F}} + C_2' \boldsymbol{\mathcal{H}}}{C_1' C_2' C_3'}, \tag{9}$$

$$\omega_o = \sqrt{\frac{C_3' \boldsymbol{\mathcal{E}} + C_1' \boldsymbol{\mathcal{F}} + C_2' \boldsymbol{\mathcal{H}}}{C_1' C_2' C_3'}}, \tag{10}$$

where $\boldsymbol{\mathcal{A}} = (g_{m3}\alpha_{p1}\alpha_{p2}\alpha_{n3}\beta_{12}\beta_{22}\beta_{31} + G_{z3}\alpha_{n1}\alpha_{n2}\beta_{11}\beta_{21})$, $\boldsymbol{\mathcal{B}} = (g_{m1}G_{z2}\alpha_{n1}\beta_{11} + g_{m2}G_{z1}\alpha_{n2}\beta_{21} + G_{z1}G_{z2})$, $\boldsymbol{\mathcal{C}} = (g_{m2}\alpha_{n2}\beta_{21} + G_{z2})$, $\boldsymbol{\mathcal{D}} = (g_{m1}\alpha_{n1}\beta_{11} + G_{z1})$, $\boldsymbol{\mathcal{E}} = (g_{m1}g_{m2}\alpha_{n1}\alpha_{n2}\beta_{11}\beta_{21} + g_{m1}G_{z2}\alpha_{n1}\beta_{11} + g_{m2}G_{z1}\alpha_{n2}\beta_{21} + G_{z1}G_{z2})$, $\boldsymbol{\mathcal{F}} = (g_{m2}G_{z3}\alpha_{n2}\beta_{21} + G_{z2}G_{z3})$, and $\boldsymbol{\mathcal{H}} = (g_{m1}G_{z3}\alpha_{n1}\beta_{11} + G_{z1}G_{z3})$.

Figure 4: The nonideal CDTA.

Table 1: Aspect ratios of the MOS in Figure 2.

MOS transistors	Aspect ratio (W/L)
M_1, M_3, M_5, M_7, M_9, M_{12}, M_{21}, M_{22}, M_{23}, M_{24}, M_{26}	27/1.8
M_2, M_4, M_6, M_8, M_{10}, M_{11}, M_{13}, M_{14}, M_{25}, M_{27}	72/1.8
M_{15}, M_{16}, M_{17}, M_{18}, M_{19}, M_{20}	63/1.8

Because the values of α and β are slightly less than unity [23], the parasitic conductances ($G_z s$) at the z terminals of CDTAs are not zero and the capacitances C_1', C_2', and C_3' are greater than C_1, C_2, and C_3, respectively. From (9) and (10), the oscillation condition and oscillation frequency are deviated from the ideal cases. Therefore, to compensate this effect, we can slightly adjust the g_{m1} or g_{m2} values. The oscillation condition still can be independently controlled by g_{m3}. The active and passive sensitivities of the quadrature oscillator are all low and obtained as

$$S^{\omega_o}_{\alpha_{n1},\alpha_{n2},\beta_{11},\beta_{21}} \cong \frac{1}{2}; \qquad S^{\omega_o}_{g_{m1},g_{m2}} \cong -S^{\omega_o}_{C_1',C_2'} \cong \frac{1}{2}; \qquad S^{\omega_o}_{C_3'} \cong 0. \tag{11}$$

4. Simulation Results

The quadrature oscillators were simulated using HSPICE. The CMOS CDTA implementation is shown in Figure 2 (using $0.18\,\mu$m MOSFET from TSMC). The aspect ratios
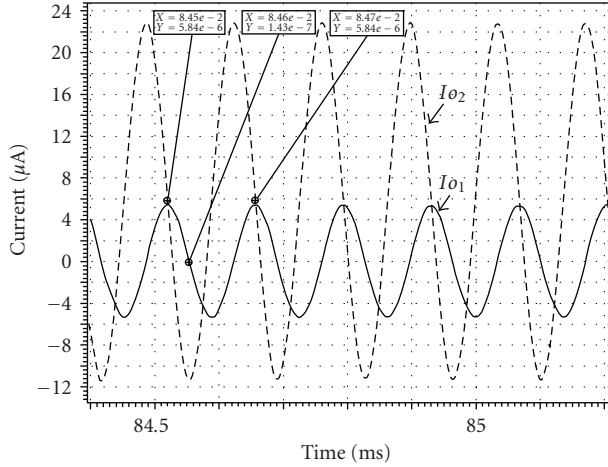
FIGURE 5: The simulated current-mode quadrature output waveforms of Figure 3.

— Theoretical
∘∘∘ Simulation

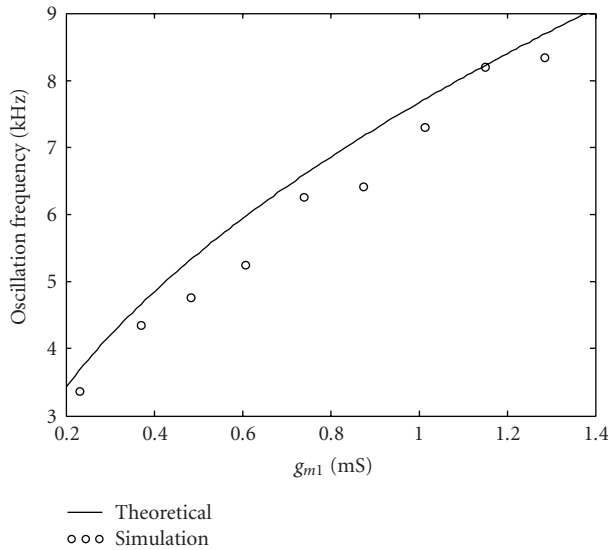FIGURE 6: Simulation results of the oscillation frequency of Figure 3, which is obtained by varying the value of the transconductance g_{m1}.

TABLE 2: Total harmonic distortion analysis of I_{o1} in Figure 3.

Harmonic no	Frequency (hz)	Fourier component	Phase (deg)
1	7.3000 k	5.3864 u	166.4101
2	14.6000 k	103.5180 n	−107.3535
3	21.9000 k	7.0925 n	−173.5386
4	29.2000 k	50.7076 n	−155.1803
5	36.5000 k	51.3941 n	106.5849
6	43.8000 k	32.4016 n	−168.3840
7	51.1000 k	41.8477 n	73.1948
8	58.4000 k	8.4629 n	120.4927
9	65.7000 k	18.1728 n	35.0011
dc component = −2.329D-09			
Total harmonic distortion = 2.5713 percent			

TABLE 3: Total harmonic distortion analysis of I_{o2} in Figure 3.

Harmonic no	Frequency (hz)	Fourier component	Phase (deg)
1	7.3000 k	17.1387 u	−103.6257
2	14.6000 k	166.8692 n	−16.1700
3	21.9000 k	11.5300 n	−138.9805
4	29.2000 k	37.8081 n	−53.1517
5	36.5000 k	35.5359 n	−162.9730
6	43.8000 k	20.2288 n	−73.4323
7	51.1000 k	14.2831 n	143.9914
8	58.4000 k	4.6312 n	177.5460
9	65.7000 k	4.5120 n	51.6697
dc component = 5.725D-06			
Total harmonic distortion = 1.0327 percent			

5. Conclusion

In this paper, a new current-mode third-order quadrature oscillator using three CDTA and three grounded capacitors is proposed. Outputs of two sinusoids with 90° phase difference are available in the proposed quadrature oscillator. The oscillation condition and oscillation frequency of the proposed quadrature oscillator are orthogonal controllable. Simulation results verify the theoretical analysis.

Acknowledgments

References

[1] A. S. Sedra and K. C. Smith, *Microelectronic Circuits*, Oxford University Press, New York, NY, USA, 4th edition, 1998.

[2] I. A. Khan and S. Khwaja, "An integrable gm-C quadrature oscillator," *International Journal of Electronics*, vol. 87, no. 11, pp. 1353–1357, 2000.

[3] R. Holzel, "Simple wide-band sine wave quadrature oscillator," *IEEE Transactions on Instrumentation and Measurement*, vol. 42, no. 3, pp. 758–760, 1993.

of the MOS transistors were chosen as in Table 1. The multiple current outputs can be easily implemented by adding output branches. Figure 5 represents the current-mode quadrature sinusoidal output waveforms of Figure 3 with $C_1 = C_2 = C_3 = 10$ nF, $g_{m1} = 1.015$ mS, $g_{m2} = 232 \mu$S, and $g_{m3} = 1.35$ mS where g_{m3} was designed to be larger than the theoretical value to ensure that the oscillations will start. The bias voltages are $V_{B1} = 0.7$ V, $V_{B2} = -0.7$ V, $V+ = 1.25$ V, and $V- = -1.25$ V. The power dissipation is 3.9486 mW. The results of the I_{o1} and I_{o2} total harmonic distortion analysis are summarized in Tables 2 and 3, respectively. Figure 6 shows the simulation results of the oscillation frequencies of Figure 3 by varying the value of the transconductance g_{m1} with $C_1 = C_2 = C_3 = 10$ nF, $g_{m2} = 232 \mu$S, and g_{m3} was varied with g_{m1} by (3) to ensures that the oscillations will start.

[4] M. T. Ahmed, I. A. Khan, and N. Minhaj, "On transconductance-C quadrature oscillators," *International Journal of Electronics*, vol. 83, no. 2, pp. 201–207, 1997.

[5] M. T. Abuelma'atti and H. A. Alzaher, "Comment on current-mode quadrature sinusoidal oscillator using single FTFN," *International Journal of Electronics*, vol. 85, no. 2, pp. 177–180, 1998.

[6] A. M. Soliman, "Synthesis of grounded capacitor and grounded resistor oscillators," *Journal of the Franklin Institute*, vol. 336, no. 4, pp. 735–746, 1999.

[7] J.-W. Horng, "Current differencing buffered amplifiers based single resistance controlled quadrature oscillator employing grounded capacitors," *IEICE Transactions on Fundamentals of Electronics, Communications and Computer Sciences*, vol. E85-A, no. 6, pp. 1416–1419, 2002.

[8] J.-W. Horng, "Current-mode quadrature oscillator with grounded capacitors and resistors using two DVCCs," *IEICE Transactions on Fundamentals of Electronics, Communications and Computer Sciences*, vol. E86-A, no. 8, pp. 2152–2154, 2003.

[9] P. Prommee and K. Dejhan, "An integrable electronic-controlled quadrature sinusoidal oscillator using CMOS operational transconductance amplifier," *International Journal of Electronics*, vol. 89, no. 5, pp. 365–379, 2002.

[10] J.-W. Horng, C.-L. Hou, C.-M. Chang, W.-Y. Chung, H.-W. Tang, and Y.-H. Wen, "Quadrature oscillators using CCIIs," *International Journal of Electronics*, vol. 92, no. 1, pp. 21–31, 2005.

[11] J.-W. Horng, C.-L. Hou, C.-M. Chang, S.-W. Pan, J.-Y. Shie, and Y.-H. Wen, "Third-order quadrature oscillator with grounded capacitors using CCIIs," *WSEAS Transactions on Electronics*, vol. 4, no. 1, pp. 20–22, 2007.

[12] S. Maheshwari and I. A. Khan, "Current controlled third order quadrature oscillator," *IEE Proceedings: Circuits, Devices & Systems*, vol. 152, no. 6, pp. 605–607, 2005.

[13] J.-W. Horng, C.-L. Hou, C.-M. Chang, H.-P. Chou, C.-T. Lin, and Y.-H. Wen, "Quadrature oscillators with grounded capacitors and resistors using FDCCIIs," *ETRI Journal*, vol. 28, no. 4, pp. 486–494, 2006.

[14] J. W. Horng, C. L. Hou, C. M. Chang, S. T. Cheng, and H. Y. Su, "Current or/and voltage-mode quadrature oscillators with grounded capacitors and resistors using FDCCIIs," *WSEAS Transactions on Circuits and Systems*, vol. 7, no. 3, pp. 129–138, 2008.

[15] A. U. Keskin, C. Aydin, E. Hancioglu, and C. Acar, "Quadrature oscillator using current differencing buffered amplifiers (CDBA)," *Frequenz*, vol. 60, no. 3-4, pp. 21–23, 2006.

[16] W. Tangsrirat and S. Pisitchalermpong, "CDBA-based quadrature sinusoidal oscillator," *Frequenz*, vol. 61, no. 3-4, pp. 102–104, 2007.

[17] A. U. Keskin and D. Biolek, "Current mode quadrature oscillator using current differencing transconductance amplifiers (CDTA)," *IEE Proceedings: Circuits, Devices & Systems*, vol. 153, no. 3, pp. 214–218, 2006.

[18] D. Biolek, "CDTA-Building block for current-mode analog signal processing," in *Proceedings of the European Conference on Circuit Theory and Design (ECCTD '03)*, vol. 3, pp. 397–400, Krakow, Poland, September 2003.

[19] A. U. Keskin, D. Biolek, E. Hancioglu, and V. Biolková, "Current-mode KHN filter employing current differencing transconductance amplifiers," *AEU-International Journal of Electronics and Communications*, vol. 60, no. 6, pp. 443–446, 2006.

[20] W. Tangsrirat and W. Tanjaroen, "Current-mode multiphase sinusoidal oscillator using current differencing transconductance amplifiers," *Circuits, Systems, and Signal Processing*, vol. 27, no. 1, pp. 81–93, 2008.

[21] D. Biolek, V. Biolkova, and A. U. Keskin, "Current mode quadrature oscillator using two CDTAs and two grounded capacitors," in *Proceedings of the 5th International Conference on System Science and Simulation in Engineering (WSEAS '06)*, pp. 368–370, Tenerife, Spain, December 2006.

[22] M. Bhusan and R. W. Newcomb, "Grounding of capacitors in integrated circuits," *Electronic Letters*, vol. 3, no. 4, pp. 148–149, 1967.

[23] A. Fabre, O. Saaid, and H. Barthelemy, "On the frequency limitations of the circuits based on second generation current conveyors," *Analog Integrated Circuits and Signal Processing*, vol. 7, no. 2, pp. 113–129, 1995.