

# FRactal CHARACTERIZATION OF LIQUID DISPERSION IN TRICKLE BED REACTOR

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## INTRODUCTION

Dispersion is very important to the design of trickle bed reactor for both chemical and biochemical processes. The degree of dispersion often influences reactor performance and scale-up. The traditional method for modeling dispersion processes in trickle bed reactors is based on the convective-diffusion equation (CDE). The most commonly used is the longitudinal-dispersion model<sup>[1, 2]</sup>. The magnitude of liquid dispersion is usually considered independent of position along the longitudinal direction of the reactor. The main assumption of the longitudinal-dispersion model is that the mixing in the axial direction follows a Fickian type of diffusion regardless of the mechanism and process involved. A constant longitudinal dispersion coefficient  $D_L$  is used to quantitatively describe all the factors making different residence time distributions RTD<sup>[3]</sup>. Recently, the above method has been questioned due to its weak theoretical background. As Westerterp *et al.* stated<sup>[4, 5]</sup>, the longitudinal-dispersion model has not been justified and it can lead to erroneous results. So the clarification on

the dispersion model and theoretical treatment is greatly desired without doubt.

It has been well accepted that porous formations (natural or artificial) may exhibit fractal structures<sup>[9, 10]</sup>. The research on the dispersion process in consolidated porous media such as soil and rocks underground, and even solid catalysts has demonstrated that dynamic processes taking place in these structures have long-range correlation<sup>[6-8, 11]</sup>. It is evident that the dispersion inside consolidated porous media is not Gaussian and can not be simply described by the CDE<sup>[6-8]</sup>. However, the trickle bed reactor used in chemical and biochemical processes belongs to unconsolidated porous media. Is there any similarity between consolidated and unconsolidated porous media with respect to liquid dispersion? The answer to this question can definitely play a vital role in clarifying the existent controversy on the longitudinal-dispersion model. Therefore, this paper is to experimentally investigate if the dispersivity is scale-dependent in trickle bed reactor at first, and then to interpret the experimental results by applying fractal analysis.

## 1 EXPERIMENTAL

The experiment was conducted with randomly packed 6 mm cylindrical particles. The packing was housed in a reactor 3.5 m in height and 70 mm in diameter. Air was blown into the reactor through a distributor at the bottom. The liquid phase,

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water, was rained in the cross section of the reactor from the top. The RTD of liquid phase was measured by a tracer injection system. The least-square method was used to fit the RTD data in order to get the model parameter. The tracer pulse was injected at one of the input ports numbered 1 to 5, along the longitudinal direction. The interval between any two neighbouring input ports is 50 cm. The nearest input port of tracer from the top is 100 cm to allow for the distribution of liquid. The injection and detection of tracer were carried out by a computer-aided system.

## 2 RESULTS AND DISCUSSION

At various liquid superficial velocities, the Peclet number  $Pe_L$  of liquid dispersion along the longitudinal direction of the reactor is presented in Fig. 1, which demonstrates an obvious non-linear dependency of  $Pe_L$  upon the superficial distance  $L_S$  between the injection point and the detecting point of tracer solution. This dependency could be expressed by a power law expression as follows

$$Pe_L = \frac{uL}{D_L} \sim L_S^\beta \quad (1)$$

Traditionally,  $Pe_L$  is only considered linearly dependent of the length scale  $L_S$ . As we know, the liquid flows down along the passages formed by random-heaped packing of catalyst pellets. The actual flow distance  $L$  is much longer than the superficial distance  $L_S$  because of the tortuosity of the flow passage. This is quite similar to the gas diffusion in porous media, so the actual length of liquid trajectory  $L$  depends on the yardstick size used for length measurement<sup>[11]</sup>. In this case, the trajectory of liquid flow can be abstracted into fractal curves, characterized by a scaling relation as shown in Eq. (1). The power in the scaling relation is the fractal dimension showing the tortuous extent of the liquid flow trajectory. The  $L$  in  $Pe_L$  should be of fractal.

By fitting the experimental results, the exponent  $\beta$  is acquired, the value of which changes from 1.57 to 1.72 with the superficial velocity

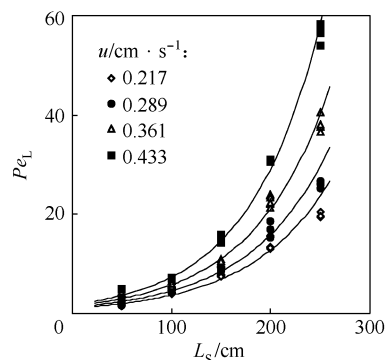


Fig. 1 Dependency of Peclet number  $Pe_L$  on superficial length scale  $L_S$

from  $0.22 \text{ m} \cdot \text{s}^{-1}$  to  $0.43 \text{ m} \cdot \text{s}^{-1}$ . The variation of exponent  $\beta$  with superficial velocity  $u$  is due to the variation of liquid pulsing because the operation of the reactor is transforming from trickling flow to pulsing flow by increasing  $u$  at a fixed gas velocity. The enhancement of liquid pulsing leads to a longer distance of liquid flow along the passages, giving rise to higher fractal dimension. The interpretation of the experimental result by computer simulations based on fluid flow in porous media and fractal geometry is well under way and will be reported in a separate article.

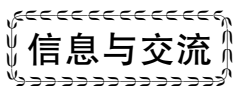
## 3 CONCLUSIONS

Experimental investigation and theoretical analysis show that the trajectory of liquid flow inside trickle bed reactors is of fractal, demonstrating that the Peclet number  $Pe_L$  of liquid dispersion in trickle bed reactors is non-linearly scale-dependant similar to what was already shown in consolidated porous media.  $Pe_L$  itself is not adequate to fully characterize the extent of liquid dispersion inside the reactor. The fractal dimension of liquid flow trajectory is a parameter showing the regularity of liquid flow inside the reactor, the value of which may be influenced by operation conditions, packing type and liquid properties.

## References

- 1 Saroha A K, Nigam K D P, Saxena A K, Dixit L. RTD Studies in Trickle Bed Reactors Packed with Porous Particles. *Can. J.*

- Chem. Eng.*, 1998, **76** (4): 738—743
- 2 Iliuta I, Larachi F, Grandjean B P A. Residence Time, Mass Transfer and Back-mixing of the Liquid in Trickle Flow Reactors Containing Porous Particles. *Chem. Eng. Sci.*, 1999, **54**: 4099—4109
  - 3 Sundaresan S, Amundson N R, Aris R. Observations on Fixed-bed Dispersion Models: the Role of the Interstitial Fluid. *AIChE J.*, 1980, **26**: 529—536
  - 4 Westerterp K R, Dilman V V, Kronberg A E. Wave Model for Longitudinal Dispersion: Development of the Model. *AIChE J.*, 1995, **41**: 2013—2028
  - 5 Westerterp K R, Dilman V V, Kronberg A E, Benneker A H. Wave Model for Longitudinal Dispersion: Analysis and Applications. *AIChE J.*, 1995, **41**: 2029—2039
  - 6 Sahimi M. Fractal and Superdiffusive Transport and Hydrodynamic Dispersion in Heterogeneous Porous Media. *Transport in Porous Media.*, 1993, **13**: 3—40
  - 7 Sahimi M. Effect of Long-Range Correlations on Transport Phenomena in Disordered Media. *AIChE J.*, 1995, **41**: 229—240
  - 8 Wheatcraft S W, Tyler S W. An Explanation of Scale-dependent Dispersivity in Heterogeneous Aquifers Using Concepts of Fractal Geometry. *Water Resour. Res.*, 1988, **24**: 566—578
  - 9 Zhang B Q, Li S F. Determination of the Surface Fractal Dimension for Porous Media by Mercury Porosimetry. *Ind. Eng. Chem. Res.*, 1995, **34**: 1383—1386
  - 10 Ghulinyan M Z, Aroutiounian V M. Structural Properties of Porous Media. *Phys. Status Solidi A*, 2003, **197** (2): 419—424
  - 11 Zhang B Q, Liu X F. Effects of Fractal Trajectory on Gas Diffusion in Porous Media. *AIChE J.*, 2003, **49**: 3037—3047



## 林纸一体化工程将带动化工发展

2月16日下午,由国家发改委组织有关部门、科研单位编制的《全国林纸一体化工程建设“十五”及2010年专项规划》,正式向全国发布。

林纸一体化是一项系统工程,对化工、包装、印刷、机械等行业具有明显的带动作用。在关闭落后草浆造纸线后,将大力发展化学木浆、化学机械木浆,并规划在东南沿海地区建设4个年产化学木浆50万吨以上的大型项目。

据介绍,造纸业与化工有着非常密切的联系,需要大量化工原料如烧碱、二氧化氯等。化学木浆是通过大量的化学及生化反应加工出溶解级木浆,除需增白以外,加工时还需化学提纯、脱树脂、解聚等;而化学机械木浆是通过机械和化学联合制浆法生产出来的木浆。这两种木浆主要采用烧碱法、硫酸盐法和亚硫酸盐法制造。这次全国林纸一体化工程建设可使化工和林业有机地结合起来,形成一条产业链。

目前世界造纸工业的总资产和销售额分别达到4000亿美元和3000亿美元,是仅次于电讯制造业和汽车工业之后的一个重要产业。2002年,我国纸及纸板消费量为4332万吨,国内产量仅为3780万吨,造纸总进口1875万吨,成为世界造纸工业中消费、生产和进口大国。到2005年我国纸及纸板消费量约5000万吨,2010年将达到7000万吨,市场潜力十分巨大。

(摘自“中国化工信息网”)