



# Goodness-of-Fit tests with Dependent Observations

Remy Chicheportiche, Jean-Philippe Bouchaud

(Submitted on 15 Jun 2011 (v1), last revised 3 Aug 2011 (this version, v2))

We revisit the Kolmogorov-Smirnov and Cramér-von Mises goodness-of-fit (GoF) tests and propose a generalisation to identically distributed, but dependent univariate random variables. We show that the dependence leads to a reduction of the "effective" number of independent observations. The generalised GoF tests are not distribution-free but rather depend on all the lagged bivariate copulas. These objects, that we call "self-copulas", encode all the non-linear temporal dependences. We introduce a specific, log-normal model for these self-copulas, for which a number of analytical results are derived. An application to financial time series is provided. As is well known, the dependence is to be long-ranged in this case, a finding that we confirm using self-copulas. As a consequence, the acceptance rates for GoF tests are substantially higher than if the returns were iid random variables.

Comments: 26 pages  
 Subjects: **Statistical Finance (q-fin.ST)**; Statistical Mechanics (cond-mat.stat-mech); Applications (stat.AP)  
 MSC classes: 91B84, 62P20, 62M10, 60F05  
 Journal reference: J. Stat. Mech. (2011) P09003  
 DOI: [10.1088/1742-5468/2011/09/P09003](https://doi.org/10.1088/1742-5468/2011/09/P09003)  
 Cite as: **arXiv:1106.3016 [q-fin.ST]**  
 (or **arXiv:1106.3016v2 [q-fin.ST]** for this version)

## Submission history

From: Remy Chicheportiche [[view email](#)]  
[\[v1\]](#) Wed, 15 Jun 2011 16:22:48 GMT (67kb)  
[\[v2\]](#) Wed, 3 Aug 2011 08:24:50 GMT (74kb)

*Which authors of this paper are endorsers?*

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

## Current browse context:

**q-fin.ST**  
[< prev](#) | [next >](#)  
[new](#) | [recent](#) | [1106](#)

## Change to browse by:

[cond-mat](#)  
[cond-mat.stat-mech](#)  
[q-fin](#)  
[stat](#)  
[stat.AP](#)

## References & Citations

- [NASA ADS](#)

## Bookmark([what is this?](#))

