

Small time expansions for transition probabilities of some Lévy processes

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Abstract

We show that there exist Lévy processes $(X_t, t \geq 0)$ and reals $y > 0$ such that for small t , the probability $P(X_t > y)$ has an expansion involving fractional powers or more general functions of t . This contrasts with previous results giving polynomial expansions under additional assumptions.

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