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The Convergence Rate of Majority Vote under Exchangeability

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Majority vote plays a fundamental role in many applications of statistics, such as ensemble classifiers, crowdsourcing, and elections. When using majority vote as a prediction rule, it is of basic interest to ask "How many votes are needed to obtain a reliable prediction?" In the context of binary classification with Random Forests or Bagging, we give a precise answer: If err_t denotes the test error achieved by the majority vote of $t \geq 1$ classifiers, and err^* denotes its nominal limiting value, then under basic regularity conditions, $\text{err}_t = \text{err}^* + c/t + o(1/t)$, where c is a constant given by a simple formula. More generally, we show that if V_1, V_2, \dots is an exchangeable Bernoulli sequence with mixture distribution F , and the majority vote is written as $M_t = \text{median}(V_1, \dots, V_t)$, then $1 - \mathbb{E}[M_t] = F(1/2) + (F''(1/2)/8)(1/t) + o(1/t)$ when F is sufficiently smooth.

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