Sampling Formulae for Symmetric Selection

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Abstract

We study partition distributions in a population genetics model incorporating symmetric selection and mutation. They generalize Ewens distributions in the infinitely-many-neutral-alleles model, an explicit expression of which is known as the Ewens sampling formula. A sampling formula for the generalized model is obtained by means of calculus for Poisson and gamma processes.

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