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## Simulated Annealing Algorithm to Minimize Makespan in Single Machine Scheduling Problem with Uniform Parallel Machines

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### ABSTRACT

This paper presents a simulated annealing algorithm to minimize makespan of single machine scheduling problem with uniform parallel machines. The single machine scheduling problem with uniform parallel machines consists of  $n$  jobs, each with single operation, which are to be scheduled on  $m$  parallel machines with different speeds. Since, this scheduling problem is a combinatorial problem; usage of a heuristic is inevitable to obtain the solution in polynomial time. In this paper, simulated annealing algorithm is presented. In the first phase, a seed generation algorithm is given. Then, it is followed by three variations of the simulated annealing algorithms and their comparison using ANOVA in terms of their solutions on makespan.

### KEYWORDS

Uniform Parallel Machines, Measure of Performance, Heuristic, Simulated Annealing Algorithm, ANOVA

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