



Generalised action-angle coordinates defined on island chains

Robert L. Dewar, Stuart R. Hudson, Ashley M. Gibson

(Submitted on 2 Apr 2012 (v1), last revised 1 Dec 2012 (this version, v2))

Straight-field-line coordinates are very useful for representing magnetic fields in toroidally confined plasmas, but fundamental problems arise regarding their definition in 3-D geometries because of the formation of islands and chaotic field regions, ie non-integrability. In Hamiltonian dynamical systems terms these coordinates are a form of action-angle variables, which are normally defined only for integrable systems. In order to describe 3-D magnetic field systems, a generalisation of this concept was proposed recently by the present authors that unified the concepts of ghost surfaces and quadratic-flux-minimising (QFMin) surfaces. This was based on a simple canonical transformation generated by a change of variable $\Theta = \theta + \zeta$ (Θ, ζ), where θ and ζ are poloidal and toroidal angles, respectively, with Θ a new poloidal angle chosen to give pseudo-orbits that are a) straight when plotted in the ζ, Θ plane and b) QFMin pseudo-orbits in the transformed coordinate. These two requirements ensure that the pseudo-orbits are also c) ghost pseudo-orbits. In the present paper, it is demonstrated that these requirements do not *uniquely* specify the transformation owing to a relabelling symmetry. A variational method of solution that removes this lack of uniqueness is proposed.

Comments: 10 pages. Accepted by Plasma Physics and Controlled Fusion as part of a cluster of refereed papers in a special issue containing papers arising from the Joint International Stellarator & Heliotron Workshop and Asia-Pacific Plasma Theory Conference, held in Canberra and Murramarang Resort, Australia, 30 January - 3 February, 2012

Subjects: **Plasma Physics (physics.plasm-ph)**; Chaotic Dynamics (nlin.CD)

Journal reference: Plasma Phys. Control. Fusion 54, 014004 (2012)

DOI: [10.1088/0741-3335/55/1/014004](https://doi.org/10.1088/0741-3335/55/1/014004)

Cite as: [arXiv:1204.0308](https://arxiv.org/abs/1204.0308) [physics.plasm-ph]
(or [arXiv:1204.0308v2](https://arxiv.org/abs/1204.0308v2) [physics.plasm-ph] for this version)

Download:

- [PDF](#)
- [Other formats](#)

Current browse context:

physics.plasm-ph

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1204](#)

Change to browse by:

[nlin](#)

[nlin.CD](#)

[physics](#)

References & Citations

- [NASA ADS](#)

Bookmark([what is this?](#))



Submission history

From: Robert L. Dewar [[view email](#)]

[v1] Mon, 2 Apr 2012 03:53:01 GMT (13kb,D)

[v2] Sat, 1 Dec 2012 02:58:13 GMT (13kb,D)

[Which authors of this paper are endorsers?](#)

Link back to: [arXiv](#), [form interface](#), [contact](#).