



Quantum Physics

# Nonlinear Boundaries in Quantum Mechanics

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(Submitted on 22 Jun 2011 (v1), last revised 1 Aug 2011 (this version, v2))

Based on empirical evidence, quantum systems appear to be strictly linear and gauge invariant. This work uses concise mathematics to show that quantum eigenvalue equations on a one dimensional ring can either be gauge invariant or have a linear boundary condition, but not both. Further analysis shows that non-linear boundaries for the ring restore gauge invariance but lead unexpectedly to eigenfunctions with a continuous eigenvalue spectrum, a discrete subset of which forms a Hilbert space with energy bands. This Hilbert space maintains the principle of superposition of eigenfunctions despite the nonlinearity. The momentum operator remains Hermitian. If physical reality requires gauge invariance, it would appear that quantum mechanics should incorporate these nonlinear boundary conditions.

Comments: 8 pages, 1 figure

Subjects: **Quantum Physics (quant-ph)**; Mathematical Physics (math-ph)

Cite as: **arXiv:1106.4510 [quant-ph]**

(or **arXiv:1106.4510v2 [quant-ph]** for this version)

## Submission history

From: Arthur Davison [[view email](#)]

[v1] Wed, 22 Jun 2011 17:16:37 GMT (173kb)

[v2] Mon, 1 Aug 2011 15:15:41 GMT (234kb)

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