

## 生灭分枝树连通分支的平均规模

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## Average Size of Connected Components in Birth-Death Branching Tree

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**摘要** 基于随机图将生物繁衍过程描述为随机图过程-随机分枝树, 建立了依赖年龄的生灭分枝树模型, 并研究了分枝树的若干拓扑性质. 首先, 给出任意节点的首生年龄和末生年龄的分布及生产年龄的顺序统计量分布. 然后, 得到以年龄 $t$ 的节点为根节点的连通分支的平均规模.

**关键词:** [随机图](#) [分枝过程](#) [生灭分枝树](#) [度分布](#) [连通分支](#)

**Abstract:** A model of age-dependent birth-death branching tree is developed based on random graph. In this model, biological reproduction processes are described as random graph processes, i.e., a random branching tree. Topological properties of the random branching tree, namely distributions of first-born and last-born age, and the distribution of order statistics of productive ages, are explored. The average size of the connected components in the branching tree is discussed.

**Keywords:** [random graph](#), [branching process](#), [birth-death branching tree](#), [degree distribution](#), [connected components](#)

收稿日期: 2012-07-10;

基金资助:

国家自然科学基金资助项目(60872060); 上海市自然科学基金资助项目(12ZR1421000); 上海市教委创新基金资助项目(12ZZ193)

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引用本文:

.生灭分枝树连通分支的平均规模[J] 上海大学学报(自然科学版), 2013,V19(2): 160-164

.Average Size of Connected Components in Birth-Death Branching Tree[J] J.Shanghai University (Natural Science Edition), 2013,V19(2): 160-164

链接本文:

<http://www.journal.shu.edu.cn//CN/10.3969/j.issn.1007-2861.2013.02.010> 或 <http://www.journal.shu.edu.cn//CN/Y2013/V19/I2/160>

[1] Harris T E. The theory of branching processes [M]. Berlin: Springer-Verlag, 1963.

[2] Athreya K B, Ney P E. Branching processes [M]. Berlin: Springer-Verlag, 1972.

[3] Bellman R, Harris T. On age-dependent binary branching processes [J]. Annals of Mathematics, 1952, 55(2): 280-295.

[4] Smith W L, Wilkinson W E. On branching processes in random environments [J]. Ann Math Statist, 1969, 40(3): 814-827.

[5] Athreya K B, Karlin S. On branching processes with random environments (I), (II) [J]. Ann Math Statist, 1971, 42(5): 1499-1520.

[6] 胡杨利, 吴庆平, 李应求. 随机环境中依赖年龄的分枝过程的爆炸问题[J]. 数学学报, 2010, 53(5): 1027-1034.

[7] 李应求, 李旭, 刘全升. 随机环境中随机游动上的随机分枝系统[J]. 中国科学: A 辑, 2007, 37(3): 341-347.

[8] 李应求, 刘全升. 随机环境中依赖年龄的分枝过程[J]. 中国科学: A 辑, 2008, 38(7): 799-818.

[9] 王汉兴. 随机环境中多物种分枝紧邻游动[J]. 科学通报, 1995, 40(7): 586-589.

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- [10] Wang H X, Dai Y L, Population-size-dependent branching processes in Markovian random environments [J]. Chinese Science Bulletin, 1998, 43 (8): 635-638.
- [11] Wang H. Extinction of P-S-D branching processes in random environments [J]. Appl Prob, 1999, 36(1): 146-154. 
- [12] Wang H X, Fang D. Asymptotic behaviour for P-S-D branching processes in Markovian random environments [J]. Appl Prob, 1999, 36(2): 611-619. 
- [13] Wang H X, Zhao F, Lu J Y. A note on asymptotic behavior of Galton-Watson branching processes in random environments [J]. Journal of Shanghai University: English Edition, 2006, 10(2): 95-99. 
- [1] 朱宏鹏;张更新;谢智东.喷泉码中LT码的次优度分布[J]. 上海大学学报(自然科学版), 2009,27(1): 6-11
- [2] A.利扎尼亚;A.戈巴利;G.多麦利;H.巴拉尼亚.半无限介质瞬态热传导的同伦分析法[J]. 上海大学学报(自然科学版), 2008,29(12): 1625-1632
- [3] 耿 普;李 超.有限域上线性码的深度分布与周期分布[J]. 上海大学学报(自然科学版), 2007,25(3): 263-263