

含有连续分布时滞偶阶微分方程的振动性

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Oscillation Criteria for Even Order Differential Equations with Continuous Distributed Delay

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摘要 本文研究了一类含有连续分布时滞偶阶中立型微分方程的振动性, 利用推广的Riccati变换和平均值技巧得到了该方程所有解均为振动的若干新的振动准则, 推广和改进了已有文献中的主要结果, 最后给出了几个例子说明结果优越性.

关键词: [振动性](#) [中立微分方程](#) [偶数阶](#)

Abstract: In this paper a class of even order neutral differential equations with continuous distributed delay are studied. By using the generalized Riccati technique and the averaging technique, we establish several new oscillation criteria for all solutions of the equations, which generalize and improve some known results. Examples are given to illustrate the superiority of our main results.

Key words: [oscillation](#) [neutral differential equations](#) [even order](#)





收稿日期: 2011-08-20;

基金资助:国家自然科学基金(11171178), 国家高等学校博士点科研基金(20103705110003)资助项目.

引用本文:

田亚州, 蔡远利, 孟凡伟. 含有连续分布时滞偶阶微分方程的振动性[J]. 应用数学学报, 2013, 36(6): 1080-1093.

TIAN Yazhou, CAI Yuanli, MENG Fanwei. Oscillation Criteria for Even Order Differential Equations with Continuous Distributed Delay[J]. Acta Mathematicae Applicatae Sinica, 2013, 36(6): 1080-1093.












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