

## 非线性不等式组的光滑近似方法及其收敛性

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## On the Convergence of Smoothing Approximate Method for Nonlinear Inequalities

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**摘要** 将非线性不等式组的求解转化成非线性最小二乘问题, 利用引入的光滑辅助函数, 构造新的极小化问题来逐次逼近最小二乘问题. 在一定的条件下, 文中所提出的光滑高斯-牛顿算法的全局收敛性得到保证. 适当条件下, 算法的局部二阶收敛性得到了证明. 文后的数值试验表明本文算法有效.

**关键词:** [非线性不等式组](#) [光滑高斯-牛顿法](#) [逐次近似](#) [全局收敛](#)

**Abstract:** Consider nonlinear inequalities, we reformulate nonlinear inequalities as nonlinear least squares problems. Using smoothing function, we construct a new optimization to approximate the least squares problems. Under some conditions, the convergence of our algorithm is proved and we analysis local quadratic rate. Numerical examples are given to illustrate our method.

**Key words:** [nonlinear inequalities](#) [smoothing Gauss-Newton method](#) [successive approximate](#) [global convergent](#)

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