

二阶奇异微分方程无穷边值问题

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Multiple Positive Solutions of Infinite Boundary Value Problem for Second-order Singular Differential Equations

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摘要 本文通过构造一个特殊的锥, 利用锥上的不动点指数原理和Krasnosel'skii不动点定理讨论了一类二阶奇异微分方程无穷边值问题正解及多重正解的存在性. 本文结果包含、推广并改进了许多已知的结果.

关键词: 无穷边值问题 二阶奇异微分方程 多重正解 不动点 锥

Abstract: In this paper, by using the fixed point principle and the Krasnosel' skii fixed point theorem, the authors discuss the existence of positive and multiple positive solutions for the singular differential equations of infinite boundary value problems in a special cone. The results significantly extend and improve many known results even for non-singular cases.

Key words: infinite boundary value problem second-order singular differential equation multiple positive solutions fixed point cone

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