

带移民和拯救的碰撞分枝过程的性质

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The Properties of Interacting Branching Collision Processes with Immigration and Resurrection

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摘要 本文考虑一类带移民和拯救的碰撞分枝过程(BCPIR)的存在唯一性、常返性以及临界爆炸情形下的衰减性质. 首先深入讨论了BCIR q -矩阵发生函数的性质, 建立了过程的唯一性判别准则, 得到了一些比较好的过程常返性充分条件; 并且通过发生函数给出了临界爆炸情形下关于连通类 Z_+ 的衰减指数 λ_Z 的精确定值. 同时, 进一步讨论 λ_Z -不变测度/不变向量, 给出了 λ_Z -不变测度的发生函数.

关键词: [碰撞分枝过程](#) [常返性](#) [衰减指数](#) [不变测度](#) [不变向量](#)

Abstract: In this paper, we consider the uniqueness, recurrence and decay properties of the Interacting Branching Collision Processes with Immigration and Resurrection (BCPIR). Some important properties of the generating functions for BC-IR q -matrix are firstly investigated in detail. It is proved that there exists a unique BCP-IR, and a good sufficient conditions for it to be recurrent is given. Moreover, the exact value of the decay parameter λ_Z is obtained in the critical explosion case. It is shown that this λ_Z can be directly given from the generating functions of the corresponding q -matrix. Finally, the λ_Z -invariant vectors/measures are presented.

Key words: [collision branching process](#) [recurrence](#) [decay parameter](#) [invariant measures](#) [invariant vectors](#)




收稿日期: 2012-06-27;

基金资助:国家自然科学基金(11071259, 90820302 和11201489);教育部高校博士点基金(20110162110060);湖南省创新基金(CX2011B077)以及中南大学基础研究基金 (2010QYZD001)资助项目.

引用本文:

王娟,李俊平. 带移民和拯救的碰撞分枝过程的性质[J]. 应用数学学报, 2013, (1): 23-37.

WANG Juan,LI Junping. The Properties of Interacting Branching Collision Processes with Immigration and Resurrection[J]. Acta Mathematicae Applicatae Sinica, 2013, (1): 23-37.









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