



给定顶点数和边数的连通图的Q-谱半径的界

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The Q-spectral radii of connected graphs with given number of vertices and edges

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摘要 图的无符号拉普拉斯矩阵是图的邻接矩阵和度对角矩阵的和, 其特征值记为 $q_1 \geq q_2 \geq \dots \geq q_n$. 设 $\mathcal{C}(n,m)$ 是由 n 个顶点 m 条边的连通图构成的集合, 这里 $1 \leq n-1 \leq m \leq \text{bigl}(\begin{smallmatrix} n \\ 2 \end{smallmatrix}\bigr)$. 图 $G^{\star} \in \mathcal{C}(n,m)$ 叫做最大图, 如果对于任意的 $G \in \mathcal{C}(n,m)$ 都有 $q_1(G^{\star}) \geq q_1(G)$ 成立. 在这篇文章中, 我们证明了对任意给定的正整数 $a=m-n+1$, 如果 $n-\frac{1}{2} + a + \frac{1}{2\sqrt{1+12a+12a^2}} \geq a + \frac{1}{2\sqrt{1+12a+12a^2}}$, 那么 $n-\frac{1}{2} + a + \frac{1}{2\sqrt{1+12a+12a^2}} \geq a + \frac{1}{2\sqrt{1+12a+12a^2}}$, 就有 $q_1(G^{\star}) \geq q_1(G)$.

关键词: 无符号拉普拉斯矩阵 最大图 嵌套分裂图, Q-谱半径

Abstract: The signless Laplacian matrix of a graph is defined to be the sum of its adjacency matrix and degree diagonal matrix, and its eigenvalues are denoted by $q_1 \geq q_2 \geq \dots \geq q_n$. Let $\mathcal{C}(n,m)$ be a set of connected graphs in which every graph has n vertices and m edges, where $1 \leq n-1 \leq m \leq \text{bigl}(\begin{smallmatrix} n \\ 2 \end{smallmatrix}\bigr)$. A graph $G^{\star} \in \mathcal{C}(n,m)$ is called maximum if $q_1(G^{\star}) \geq q_1(G)$ for any $G \in \mathcal{C}(n,m)$. In this paper, we proved that for any given positive integer $a=m-n+1$, $n-\frac{1}{2} + a + \frac{1}{2\sqrt{1+12a+12a^2}} \geq a + \frac{1}{2\sqrt{1+12a+12a^2}}$, which leads to $q_1(G^{\star}) \geq q_1(G)$.

Keywords: signless Laplacian, maximum graph, nested split graph, Q-spectral radius

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