

## 基于动态VaR约束与随机波动率模型的最优投资策略

伊博<sup>1</sup>, 李仲飞<sup>2,3</sup>, 曾燕<sup>2,3</sup>

1. 中山大学数学与计算科学学院, 广州, 510275; 2. 中山大学岭南(大学)学院, 广州, 510275; 3. 中山大学金融工程与风险管理研究中心, 广州, 510275

## Optimal investment strategy with stochastic volatility and dynamic VaR constraint

YI Bo<sup>1</sup>, LI Zhong-Fei<sup>2,3</sup>, ZENG Yan<sup>2,3</sup>

1. School of Mathematics and Computational Science, Sun Yat-sen University, Guangzhou 510275, China; 2. Lingnan (University) College, Sun Yat-sen University, Guangzhou 510275, China; 3. Research Center for Financial Engineering and Risk Management, Sun Yat-sen University, Guangzhou 510275, China

- 摘要
- 参考文献
- 相关文章

Download: PDF (242KB) [HTML](#) (1KB) Export: BibTeX or EndNote (RIS) [Supporting Info](#)

**摘要** 研究Stein-Stein随机波动率模型下带动态VaR约束的最优投资组合选择问题. 假设投资者的目标是最大化终端财富的期望幂效用, 可投资于无风险资产和一种风险资产, 风险资产的价格过程由Stein-Stein随机波动率模型刻画. 同时, 投资者期望能在投资过程中利用动态VaR约束控制所面对的风险. 运用Bellman动态规划方法和Lagrange乘子法, 得到了该约束问题最优策略的解析式及特殊情形下最优值函数的解析式; 并通过理论分析和数值算例, 阐述了动态VaR约束与随机波动率对最优投资策略的影响.

**关键词:** 动态VaR约束 随机波动率 最优投资策略 动态规划 效用最大化

**Abstract:** This paper considers an optimal portfolio choice problem under Stein-Stein stochastic volatility model and dynamic VaR constraint. The investor aims to maximize the expected power utility of the terminal wealth, and the financial market consists of one risk-free asset and one risky asset whose price process is described by Stein-Stein stochastic volatility model. At the same time, the investor hopes to limit the potential risk over investment horizon by a dynamic VaR constraint. Adopting the stochastic dynamic programming approach and Lagrange multiple method, we derive the closed-form expressions of the optimal strategy as well as the optimal value function in a special case. Moreover, economic implications and numerical analysis are proposed to illustrate the impacts of stochastic volatility and dynamic VaR constraint on the investor's optimal strategy.

**Keywords:** dynamic VaR constraint, stochastic volatility, optimal portfolio strategy, dynamic programming, utility maximization

收稿日期: 2011-08-24; 出版日期: 2012-06-15

基金资助:

国家杰出青年科学基金(No. 70825002), 教育部人文社会科学研究青年基金(No. 12YJCZH267), 广东省哲学社会科学规划项目(No. GD11YYJ07)

通讯作者 李仲飞 Email: Inslzf@mail.sysu.edu.cn

引用本文:

伊博, 李仲飞, 曾燕. 基于动态VaR约束与随机波动率模型的最优投资策略[J] 运筹学学报, 2012, V16(2): 77-90


YI Bo, LI Zhong-Fei, ZENG Yan. Optimal investment strategy with stochastic volatility and dynamic VaR constraint[J] OR TRANSACTIONS, 2012, V16(2): 77-90

链接本文:

http://202.120.127.195/shu\_ycxxb/CN/ 或 http://202.120.127.195/shu\_ycxxb/CN/Y2012/V16/I2/77

[1] Markowitz H M. Portfolio selection [J]. Journal of Finance, 1952, 7: 77-91.

[2] Merton R C. Optimum consumption and portfolio rules in a continuous-time model [J]. Journal of Economic Theory, 1971, 69: 401-430.

[3] Li D, Ng W L. Optimal dynamic portfolio selection: Multiperiod Mean-Variance formulation [J]. Mathematical Finance, 2000, 10(3): 387-406. 

[4] Zhou X Y, Li D. Continuous-time Mean-Variance portfolio selection: a stochastic LQ framework [J]. Applied Mathematics and Optimization,

### Service

- ▶ 把本文推荐给朋友
- ▶ 加入我的书架
- ▶ 加入引用管理器
- ▶ Email Alert
- ▶ RSS

### 作者相关文章

- ▶ 伊博
- ▶ 李仲飞
- ▶ 曾燕

- [5] Stein E M, Stein J C. Stock price distributions with stochastic volatility:an analytic approach [J]. Review of Financial Studies, 1991, 4: 725-752.
- [6] Heston S L. A closed-form solution for options with stochastic volatility with applications to bond and currency options [J]. Review of Financial Studies, 1993, 6: 327-343. 
- [7] Liu J, Pan J. Dynamic derivative strategies [J]. Journal of Financial Economics, 2003, 69: 401-430. 
- [8] Chacko G, Viceira L M. Dynamic consumption and portfolio choice with stochastic volatility in incomplete markets [J]. Review of Financial Studies, 2005, 18: 1369-1402. 
- [9] Duffie D, Epstein L G. Asset pricing with stochastic differential utility [J]. Review of Financial Studies, 1992, 5(3): 411-436. 
- [10] Hsuku Y. Dynamic consumption and asset allocation with dericative securities [J]. Quantitative Finance, 2007, 7(2): 137-149. 
- [11] Roy A D. Safety first and the holding of assets [J]. Econometrica: Journal of the Econometric Society, 1952, 20(3): 431-499.
- [12] Basak S, Shapiro A. Value-at-risk-based risk management: optimal policies and asset prices [J]. The Review of Financial Studies, 2001, 14(2): 371-405. 
- [13] Jorion P. Value at Risk [M]. New york: McGraw-Hill, 2001.
- [14] Yiu K F C. Optimal portfolios under a value-at-risk constraint [J]. Journal of Economic Dynamics & Control, 2004, 28: 1317-1334. 
- [15] Cuoco D, He H, Issaenko S. Optimal dynamic trading strategies with risk limits [J]. Operational Research, 2008, 56(2): 358-368.
- [16] Chen S M, Li Z F, Li K M. Optimal investment-reinsurance policy for an insurance company with VaR constraint [J]. Insurance: Mathematics and Economics, 2010, 47: 144-153. 
- [17] Pirvu T A. Portfolio optimization under the Value-at-Risk constraint [J]. Quantitative Finance, 2007, 7: 125-136. 
- [18] 李仲飞, 李克勉. 动态VaR约束下带随机波动的衍生证券最优投资策略[J]. 中山大学学报(社会科学版), 2010, 50(3): 184-192.
- [1] 张鹏.连续型动态规划的新算法研究[J]. 运筹学学报, 2012,16(1): 97-105