

# Turkish Journal of Mathematics

Turkish Journal

of

Mathematics

Some Asymptotic Results for the Semi-Markovian Random Walk with a Special Barrier

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**Abstract:** In this study, the semi-Markovian random walk with a special barrier  $(X(t))$  is considered and under some weak assumptions the ergodicity of this process is discussed. Moreover, the characteristic function of ergodic distribution of  $X(t)$  is given by using a joint distribution of random variables  $N$  and  $Y_N$  and some exact formulas for the first and second moments of ergodic distribution of the process  $X(t)$  are obtained. Based on these results, the asymptotic behaviours of expectation and variance of this process are investigated as  $S \rightarrow \infty$ . It is finally proved that the ergodic distribution of the process is close to a uniform distribution over  $(s, S)$  as  $S$  takes sufficiently large values.

**Key Words:** Semi-Markovian random walk; ergodicity of process; asymptotic behaviour; weakly convergence

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Turk. J. Math., **27**, (2003), 251-271.

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Other articles published in the same issue: [Turk. J. Math., vol.27, iss.2.](#)