

The scaling limit of the critical one-dimensional random Schrodinger operator

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We consider two models of one-dimensional discrete random Schrodinger operators $(H_n \psi)_l = \psi_{l-1} + \psi_{l+1} + v_l \psi_l$, $\psi_0 = \psi_{n+1} = 0$ in the cases $v_k = \sigma \omega_k / \sqrt{n}$ and $v_k = \sigma \omega_k / \sqrt{k}$. Here ω_k are independent random variables with mean 0 and variance 1.

We show that the eigenvectors are delocalized and the transfer matrix evolution has a scaling limit given by a stochastic differential equation. In both cases, eigenvalues near a fixed bulk energy E have a point process limit. We give bounds on the eigenvalue repulsion, large gap probability, identify the limiting intensity and provide a central limit theorem.

In the second model, the limiting processes are the same as the point processes obtained as the bulk scaling limits of the beta-ensembles of random matrix theory. In the first model, the eigenvalue repulsion is much stronger.

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