



Mathematics > Probability

# Pointwise stabilization of discrete-time matrix-valued stationary Markov chains

Xiongping Dai, Yu Huang, Mingqing Xiao

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Let  $(\Omega, \mathscr{F}, \mathbb{P})$  be a probability space and  $\mathbb{S} = \{\mathrm{S}_1, \dots, \mathrm{S}_K\}$  a discrete-topological space that consists of  $K$  real  $d$ -by- $d$  matrices, where  $K$  and  $d$  both  $\geq 2$ . In this paper, we study the pointwise stabilizability of a discrete-time, time-homogeneous, stationary  $(\mathbb{P})$ -Markovian jump linear system  $\{X_n = (x_n)_{n=1}^{+\infty}\}$  where  $x_n \in \Omega \rightarrow \mathbb{S}$ . Precisely,  $\{X_n\}$  is called "pointwise convergent", if to any initial state  $x_0 \in \mathbb{R}^{1 \times d}$ , there corresponds a measurable set  $\Omega_{x_0} \subset \Omega$  with  $\mathbb{P}(\Omega_{x_0}) > 0$  such that  $\prod_{\ell=1}^n x_{\ell}(\omega) \rightarrow \mathbf{0}_{1 \times d}$  as  $n \rightarrow +\infty$ ,  $\forall \omega \in \Omega_{x_0}$ ;  $\{X_n\}$  is said to be "pointwise exponentially convergent", if to any initial state  $x_0 \in \mathbb{R}^{1 \times d}$ , there corresponds a measurable set  $\Omega'_{x_0} \subset \Omega$  with  $\mathbb{P}(\Omega'_{x_0}) > 0$  such that  $\prod_{\ell=1}^n x_{\ell}(\omega) \rightarrow \mathbf{0}_{1 \times d}$  exponentially fast as  $n \rightarrow +\infty$ ,  $\forall \omega \in \Omega'_{x_0}$ . Using dichotomy, we show that if  $\{X_n\}$  is product bounded, i.e.,  $\exists \beta > 0$  such that  $\prod_{\ell=1}^n x_{\ell}(\omega) \leq \beta \mathbf{1}_{2 \times 2}$  for all  $n \geq 1$  and  $\mathbb{P}$ -a.e.  $\omega \in \Omega$ ; then  $\{X_n\}$  is pointwise convergent if and only if it is pointwise exponentially convergent.

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