论文

关于弱压缩算子的变分不等式解的粘滞逼近算法

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摘要：

在严格凸且具有一致Gâteaux可微范数的Banach空间E框架内, 该文借助于两种粘滞逼近算法去近似逼近关于弱压缩算子的变分不等式解并且也获得了相应的收敛率估计.

关键词： 粘滞逼近算法　非扩张映射序列　弱压缩算子　收敛率估计　严格凸Banach空间

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Solving Variational Inequality with Weak Contraction by Using Viscosity Approximation Methods

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Abstract:

In this paper, under the framework of a strictly convex Banach space with a uniformly Gâteaux differentiable norm, we study strong convergence of two explicit viscosity approximation methods for finding a solution to the variational inequality with weakly contractive mapping A, and give the estimate of convergence rate.

Keywords: Viscosity approximation methods　Nonexpansive mappings sequence　Weak contractions　The estimate of convergence rate　Strictly convex Banach space

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