



# Good measures on locally compact Cantor sets

O. Karpel

(Submitted on 30 Mar 2012)

We study the set  $M(X)$  of full non-atomic Borel (finite or infinite) measures on a non-compact locally compact Cantor set  $X$ . For an infinite measure  $\mu$  in  $M(X)$ , the set  $\mathfrak{M}_\mu = \{x \in X : \text{for any compact open set } U \ni x \text{ we have } \mu(U) = \infty\}$  is called defective. We call  $\mu$  non-defective if  $\mu(\mathfrak{M}_\mu) = 0$ . The class  $M^0(X) \subset M(X)$  consists of probability measures and infinite non-defective measures. We classify measures  $\mu$  from  $M^0(X)$  with respect to a homeomorphism. The notions of goodness and compact open values set  $S(\mu)$  are defined. A criterion when two good measures from  $M^0(X)$  are homeomorphic is given. For any group-like  $D \subset [0,1)$  we find a good probability measure  $\mu$  on  $X$  such that  $S(\mu) = D$ . For any group-like  $D \subset [0,\infty)$  and any locally compact, zero-dimensional, metric space  $A$  we find a good non-defective measure  $\mu$  on  $X$  such that  $S(\mu) = D$  and  $\mathfrak{M}_\mu$  is homeomorphic to  $A$ . We consider compactifications  $cX$  of  $X$  and give a criterion when a good measure  $\mu \in M^0(X)$  can be extended to a good measure on  $cX$ .

Comments: 21 pages

Subjects: **Dynamical Systems (math.DS)**

MSC classes: 37A05, 37B05 (Primary), 28D05, 28C15 (Secondary)

Cite as: **arXiv:1204.0027 [math.DS]**

(or **arXiv:1204.0027v1 [math.DS]** for this version)

## Submission history

From: Olena Karpel [[view email](#)]

[v1] Fri, 30 Mar 2012 21:25:40 GMT (17kb)

[Which authors of this paper are endorsers?](#)

Link back to: [arXiv](#), [form interface](#), [contact](#).

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

Current browse context:

math.DS

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1204](#)

Change to browse by:

[math](#)

## References & Citations

- [NASA ADS](#)

Bookmark([what is this?](#))

