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## 某些四阶时滞微分方程解的稳定性

西密尔·通兹

玉珍翠延大学 文学与科学学院 数学系, 凡城 65080 土耳其

**摘要:** 利用Liapunov函数法, 得到了一个新的、证明某些四阶非线性时滞微分方程零解渐近稳定的结果. 建立结果的限制性条件弱于其他文献给出的方法.

**关键词:** 四阶非线性时滞微分方程; 稳定性; Liapunov泛函

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**作者简介:**

C·通兹(cemtunc@yahoo.com).

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