



Mathematics > Number Theory

# On Colmez's product formula for periods of CM-abelian varieties

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Colmez conjectured a product formula for periods of abelian varieties with complex multiplication by a field  $K$ , analogous to the standard product formula in algebraic number theory. He proved this conjecture up to a rational power of 2 for  $K/\mathbb{Q}$  abelian. In this paper, we complete the proof of Colmez for  $K/\mathbb{Q}$  abelian by eliminating this power of 2. Our proof relies on analyzing the Galois action on the De Rham cohomology of Fermat curves in mixed characteristic  $(0, 2)$ , which in turn relies on understanding the stable reduction of  $Z/2^n$ -covers of the projective line, branched at three points.

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