



# The KH-Theory of Complete Simplicial Toric Varieties and the Algebraic K-Theory of Weighted Projective Spaces

Adam Massey

(Submitted on 30 Jun 2012 (v1), last revised 3 Jul 2012 (this version, v2))

We show that, for a complete simplicial toric variety  $X$ , we can determine its homotopy  $K$ -theory (denoted  $KH$ -theory) entirely in terms of the torus pieces of open sets forming an open cover of  $X$ . We accomplish this by constructing a simplicial scheme  $\text{BOT}_X$  and constructing a relationship between the spectrum  $KH(X)$  and a certain spectrum determined by  $\text{BOT}_X$ . We then construct conditions under which, given two complete simplicial toric varieties with the same simplicial structure, the two spectra  $KH(X) \otimes \mathbb{Q}$  and  $KH(Y) \otimes \mathbb{Q}$  are weakly equivalent. We apply this result to determine the rational  $KH$ -theory of weighted projective spaces. We next examine  $K$ -regularity for complete toric surfaces; in particular, we show that complete toric surfaces (and therefore 2-dimensional weighted projective spaces) are  $K_0$ -regular. We then determine conditions under which our approach for dimension 2 works in arbitrary dimensions, before demonstrating that weighted projective spaces are not  $K_1$ -regular, and for dimensions bigger than 2 are also not in general  $K_0$ -regular.

Comments: 24 pages. Updated version, correcting significant typos in the first version

Subjects: **K-Theory and Homology (math.KT)**; Algebraic Geometry (math.AG)

MSC classes: 19D10

Cite as: **arXiv:1207.0123 [math.KT]**  
(or **arXiv:1207.0123v2 [math.KT]** for this version)

## Submission history

From: Adam Massey [[view email](#)]

[v1] Sat, 30 Jun 2012 18:17:13 GMT (40kb)

[v2] Tue, 3 Jul 2012 08:49:36 GMT (40kb)

*Which authors of this paper are endorsers?*

## Download:

- [PDF](#)
- [PostScript](#)
- [Other formats](#)

Current browse context:

math.KT

[< prev](#) | [next >](#)

[new](#) | [recent](#) | [1207](#)

Change to browse by:

[math](#)

[math.AG](#)

## References & Citations

- [NASA ADS](#)

Bookmark([what is this?](#))



