



Mathematics > Group Theory

# The first $L^2$ -Betti number and approximation in arbitrary characteristic

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Let  $G$  be a finitely generated group and  $(G_i)$  a descending chain of finite index normal subgroups of  $G$ . Given a field  $K$ , we consider the sequence  $b_1(G_i; K)/[G:G_i]$  of normalized first Betti numbers of  $G_i$  with coefficients in  $K$ , which we call a  $K$ -approximation for  $b_1^{(2)}(G)$ , the first  $L^2$ -Betti number of  $G$ . In this paper we address the questions of when  $Q$ -approximation and  $F_p$ -approximation have a limit, when these limits coincide, when they are independent of the sequence  $(G_i)$  and how they are related to  $b_1^{(2)}(G)$ . In particular, we show that the limit of the sequence  $b_1(G_i; F_p)/[G:G_i]$  is greater than or equal to  $b_1^{(2)}(G)$  under the assumptions that  $(G_i)$  has trivial intersection and each  $G/G_i$  is a finite  $p$ -group.

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