# New properties of multiple harmonic sums modulo \$p\$ and \$p\$-analogues of Leshchiner's series 

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In this paper we present some new identities of hypergeometric type for multiple harmonic sums whose indices are the sequences $\left.\$(\backslash\{1\}\}^{\wedge} a, c, \backslash\{1 \backslash\}^{\wedge} b\right), \$$ $\left.\$\left(\backslash\{2 \mid\}^{\wedge} a, c, \backslash\{2\}\right\}^{\wedge} b\right) \$$ and prove a number of congruences for these sums modulo a prime \$p.\$ The congruences obtained allow us to find nice \$p\$analogues of Leshchiner's series for zeta values and to refine a result due to M. Hoffman and J. Zhao about the set of generators of the multiple harmonic sums of weight 7 and 9 modulo $\$ p \$$. Moreover, we are also able to provide a new proof of Zagier's formula for \$lzeta^\{*\}(<br>{2\}\}^a,3,<br>{2|\}^b)\$ based on a finite } identity for partial sums of the zeta-star series.

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