



High Energy Physics - Theory

# Enhanced Gauge Groups in N=4 Topological Amplitudes and Lorentzian Borcherds Algebras

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We continue our study of algebraic properties of N=4 topological amplitudes in heterotic string theory compactified on  $T^2$ , initiated in [arXiv:1102.1821](#). In this work we evaluate a particular one-loop amplitude for any enhanced gauge group  $\mathfrak{h} \subset \mathfrak{e}_8 + \mathfrak{e}_8$ , i.e. for arbitrary choice of Wilson line moduli. We show that a certain analytic part of the result has an infinite product representation, where the product is taken over the positive roots of a Lorentzian Kac-Moody algebra  $\mathfrak{g}^{\{++\}}$ . The latter is obtained through double extension of the complement  $\mathfrak{g} = (\mathfrak{e}_8 + \mathfrak{e}_8)/\mathfrak{h}$ . The infinite product is automorphic with respect to a finite index subgroup of the full T-duality group  $SO(2,18;\mathbb{Z})$  and, through the philosophy of Borcherds-Gritsenko-Nikulin, this defines the denominator formula of a generalized Kac-Moody algebra  $G(\mathfrak{g}^{\{++\}})$ , which is an 'automorphic correction' of  $\mathfrak{g}^{\{++\}}$ . We explicitly give the root multiplicities of  $G(\mathfrak{g}^{\{++\}})$  for a number of examples.

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